

Combinational Logic Design Process

- Create truth table from specification
- Generate K-maps & obtain logic equations
- Draw logic diagram (sharing common gates)
- Simulate circuit for design verification
 - Debug & fix problems when output is incorrect
 - Check truth table against K-map population
 - Check K-map groups against logic equation product terms
 - Check logic equations against schematic
- Circuit optimization for area and/or performance
 - Analyze verified circuit for optimization metric
 - G , G_{IO} , G_{del} , P_{del}
 - Use Boolean postulates & theorems
- Re-simulate & verify optimized design

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Circuit Analysis

- We can implement different circuits for same logic function that are *functionally equivalent* (produce the correct output response for all input values)
 - Which implementation is the best?
 - Depends on design goals and criteria
- Area analysis
 - Number of gates, G (most commonly used)
 - Number of gate inputs and outputs, G_{IO} (more accurate)
 - Bigger gates take up more area
- Performance analysis (*worst case path from inputs to outputs*)
 - Number of gates in worst case path from input to output, G_{del}
 - More accurate delay measurement per gate
 - Propagation delay = intrinsic (*internal*) delay + extrinsic (*external*) delay
 - Relative prop delay, $P_{del} = \# \text{ inputs to gate (intrinsic)} + \# \text{ loads (extrinsic)}$

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K-mapping & Minimization Steps

Step 1: generate K-map

- Put a 1 in all specified minterms
- Put a 0 in all other boxes (optional)

Step 2: group all adjacent 1s without including any 0s

- All groups (aka *prime implicants*) must be rectangular and contain a “power-of-2” number of 1s
 - 1, 2, 4, 8, 16, 32, ...
- An essential group (aka *essential prime implicant*) contains at least 1 minterm not included in any other groups
 - A given minterm may be included in multiple groups

Step 3: define product terms using variables common to all minterms in group

Step 4: sum all essential groups plus a minimal set of remaining groups to obtain a minimum SOP

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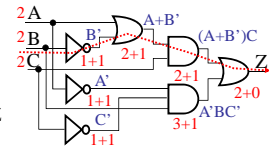
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Circuit Analysis Example

- From previous example:

$$Z = (A+B')C + A'BC'$$

- # gates: $G = 7$
- # gate I/O: $G_{IO} = 19$
- Gate delay: $G_{del} = 4$
 - worst case path: $B \rightarrow Z$
- Prop delay: $P_{del} = 12$
 - worst case path: $B \rightarrow Z$



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K-map Minimization Goals

- Larger groups:
 - Smaller product terms
 - Fewer variables in common
 - Smaller AND gates
 - In terms of number of inputs
- Fewer groups:
 - Fewer product terms
 - Fewer AND gates
 - Smaller OR gate
 - In terms of number of inputs
- Alternate method:
 - Group 0s
 - Could produce fewer and/or smaller product terms
 - Invert output
 - Use NOR instead of OR gate

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Design Verification Guidelines

- Use all audits and analysis aids possible to help find potential design bugs
 - Investigate and correct all errors/warnings
- Simulate thoroughly but use stimuli that “eat their way into the design” testing one function at a time
 - more important for complex circuits
- When circuit doesn’t work, see what works and what doesn’t to narrow down the search space for the problem
 - Which outputs work
 - Which outputs fail and under what conditions
 - Monitor lots of internal nodes
 - Additional simulations (with different vectors) can be helpful
- “Debugging is just like solving a puzzle”
 - “If something doesn’t look right, stop and check it out”
 - Don’t overlook potential bugs
 - “When you’ve found the problem, everything starts makes sense”
- Always re-run audits and simulation after correcting any problem (or after making any changes)
 - Another bug could be lurking, or
 - The fix may have messed up something else

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Sequential Logic Design Steps

- Derive circuit state diagram from design specs
- Create state table
- Choose flip-flops (D, T, SR, JK)
- Create circuit excitation table
 - use flip-flop excitation tables
- Construct K-maps for:
 - flip-flop inputs
 - primary outputs
- Obtain minimized SOP equations
- Draw logic diagram
- Simulate to verify design & debug as needed
- Perform circuit analysis & logic optimization

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3-bit Gray Code Counter

- Choose flip-flops:
 - Let X be a JK
 - Let Y be a D
 - Let Z be a SR
- Create circuit excitation table

Inputs R	Current state (X Y Z)	Next state (X Y Z)	QX Jx Kx	QY Dy	QZ Sz Rz
0	X X X	0 0 0	0 1	0	0 1
1	0 0 0	0 0 1	0 X	0	1 0
1	0 0 1	0 1 1	0 X	1	X 0
1	0 1 0	1 1 0	1 X	1	0 X
1	0 1 1	0 1 0	0 X	1	0 1
1	1 0 0	0 0 0	X 1	0	0 X
1	1 0 1	1 0 0	X 0	0	0 1
1	1 1 0	1 1 1	X 0	1	1 0
1	1 1 1	1 0 1	X 0	0	X 0

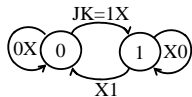
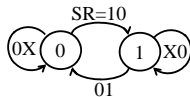
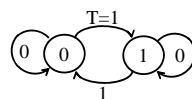
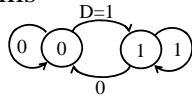
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Flip-Flop Excitation Tables & State Diagrams

Q Q+	D	T	SR	JK
0 0	0	0	0X	0X
0 1	1	1	10	1X
1 0	0	1	01	X1
1 1	1	0	X0	X0



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3-bit Gray Code Counter (cont)

- Generate K-Maps & obtain minimized SOPs

RX \ YZ	00	01	11	10
00				
01				
11	X	X	X	X
10				1

$$J_x = RYZ'$$

RX \ YZ	00	01	11	10
00				
01				
11				1
10				1

$$D_y = RYZ' + RX'Z$$

RX \ YZ	00	01	11	10
00				
01				
11			X	1
10			1	X

$$S_z = RXY + RX'Y'$$

RX \ YZ	00	01	11	10
00		1	1	1
01		1	1	1
11	1	0	0	0
10	X	X	X	X

$$K_x = R' + Y'Z'$$

Further reductions:

$$R_z = R' + X \oplus Y$$

$$S_z = R(X \oplus Y)'$$

$$= (R' + X \oplus Y)'$$

$$= R_z'$$

RX \ YZ	00	01	11	10	
00		1	1	1	
01		1	1	1	
11	X	1			
10				1	X

$$R_z = R' + XY' + X'Y$$

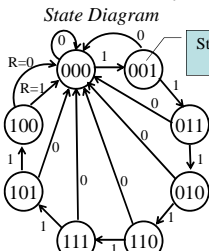
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Sequential Design Example

Design a 3-bit gray code counter with active low synchronous reset (R)



Inputs R	Current state (X Y Z)	Next state (X Y Z)
0	XXX	000
1	000	001
1	001	011
1	010	110
1	011	010
1	100	000
1	101	100
1	110	111
1	111	101

State Table

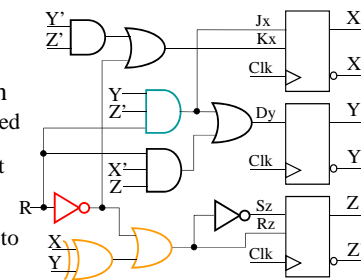
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3-bit Gray Code Counter (cont)

- Logic diagram
- Then design verification via logic simulation
 - Debug as needed to obtain working circuit
 - Update logic diagram, logic equations, etc. to reflect fixes



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Sequential Logic Models

- Huffman model consists of two types:
 - Mealy model (aka Mealy machine)
 - Outputs are function inputs and current state
 - Outputs can change when inputs change or when current state changes
 - Moore model (aka Moore machine)
 - Outputs are function of current state only
 - Outputs can change only when current state changes

only for Mealy

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Mealy & Moore Design Examples

In this example the D_x and D_y circuits are the same for both Mealy and Moore. But the outputs circuits are different with the Moore being a function of X and Y only.

X Y

In	00	01	11	10
0	0	1	X	0
1	1	0	X	0

$D_x = In'Y + InX'Y'$

X Y

In	00	01	11	10
0	1	0	X	1
1	1	1	X	0

$O_{Mealy} = In'Y' + InX'$

X Y

In	00	01	11	10
0	1	0	X	0
1	0	0	X	1

$D_y = InX + In'X'Y'$

X Y

In	00	01	11	10
0	1	0	X	0
1	1	0	X	0

$O_{Moore} = X'Y'$

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Mealy & Moore State Diagrams

- Mealy model**
 - Outputs associated with state transition
 - Output values shown with inputs
- Moore model**
 - Outputs associated with states only
 - Output values shown with states

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Mealy & Moore Design Examples

$O_{Mealy} = In'Y' + InX'$

$D_x = In'Y + InX'Y'$

$D_y = InX + In'X'Y'$

$O_{Moore} = X'Y'$

Note: O_{Mealy} is a function of In but O_{Moore} is not a function of In.

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Mealy & Moore State Tables

In	X	Y	X ⁺	Y ⁺	D _X	D _Y	O _{Mealy}	O _{Moore}
0	0	0	0	1	0	1	1	1
0	0	1	1	0	1	0	0	0
0	1	0	0	0	0	0	1	0
1	0	0	1	0	1	0	1	1
1	0	1	0	0	0	0	1	0
1	1	0	0	1	0	1	0	0
0	1	1	X	X	X	X	X	X

Note: next state (next state logic) is same for both Mealy & Moore – only output is different

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Flip-Flop Initialization

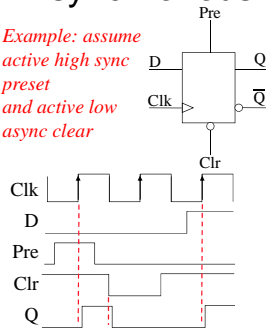
- Preset (aka set) $\Rightarrow Q^+ = 1$
- Clear (aka reset) $\Rightarrow Q^+ = 0$
- Some flip-flops have:
 - Both preset and clear (set and reset)
 - A preset or a clear
 - Neither (JK & SR flops have set/reset functions)
- Preset and/or clear can be
 - Active high or active low
 - Synchronous \Rightarrow with respect to active edge of clock
 - Asynchronous \Rightarrow independent of clock edges
- Initialization important for:
 - logic simulation to remove undefined logic values
 - 2, 3, U, etc.
 - system operation to put system in a known state

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Synchronous vs. Asynchronous

- Synchronous => states of memory elements change only with respect to active edge of clock
- Asynchronous => states of memory elements can change without an active edge of clock
 - Asynchronous designs often have timing problems

Example: assume active high sync preset and active low async clear



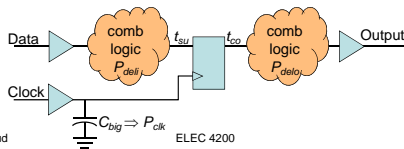
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System-Level Timing

- System set-up time: $P_{deli} + P_{bufi} + t_{su} - P_{clk(min)}$
 - > $P_{deli} + P_{bufi} + t_{su}$
- System hold time: $t_h + P_{clk} - P_{deli(min)} - P_{bufi(min)}$
 - > $t_h + P_{clk}$
- System clock-to-output: $t_{co} + P_{delo} + P_{bufo} + P_{clk}$
- **Minimum times are difficult to guarantee**
 - Typically assume 0



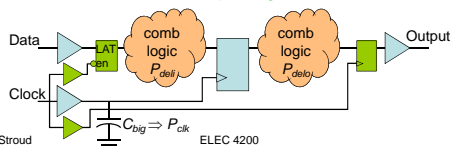
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System-Level Timing

- System set-up time: $P_{bufi} + t_{su(latch)} - P_{clk(input)min}$
- System hold time: $t_h(latch) + P_{clk(input)} - P_{bufi(min)}$
- System clock-to-output: $t_{co} + P_{bufo} + P_{clk(output)}$
- **Improvement techniques:**
 - Re-clock signals onto/off subcircuit, chip, PCB, or system
 - Fanout clock into input, main, and output clocks
 - 0-hold-time latches on input signals



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