

Use of Vision Sensors and Lane Maps to Aid GPS-INS under a Limited GPS Satellite Constellation



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Work Funded by FHWA

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Outline

- Prior Work/Contributions
- Motivation
- Background
- Lane Map
- 6DOF Filter Setup and Results
- Limited GPS Satellite Observability and Results



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Motivation

- Research has shown that nearly half of traffic fatalities occur due to an unintentional lane departure.
 - Lane departure warning (LDW) systems may prevent many of these accidents.
 - Current LDW systems use only vision sensors.
- GPS based navigation filters are prone to failure in urban environments.
- Goal of this thesis is to present a method of combining vision measurements and vehicle constraints to maintain observability of a GPS based navigation filter when only 2 GPS satellites are visible.
- An Extended Kalman Filter is used to combine measurements from a GPS receiver, LiDAR, camera, and IMU.
 - The navigation coordinate frame used is a Cartesian coordinate frame based off a waypoint map.



Prior Work

- J. Clanton, "Gps and inertial sensors enhancement for vision-based highway lane tracking," Master's thesis, Auburn University, 2006.
- S. Mammarr, S. Glaser, and M. Netto, "Time to line crossing for lane departure avoidance: a theoretical study and an experimental setting," vol. 7, no. 2, pp. 226-241, 2006.
- J. Kibbel, W. Justus, and K. Furstenberg, "Lane estimation and departure warning using multilayer laserscanner," in Proc. IEEE Intelligent Transportation Systems, pp. 607-611, 2005.



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Contributions

- J. W. Allen and D. M. Bevly, "Use of vision sensors and lane maps to aid gps/ins under a limited gps satellite constellation," in 2010 ION GNSS Savannah, Georgia, 2010.
- J. W. Allen and D. M. Bevly, "Relating local vision measurements to global navigation satellite systems using waypoint based maps," in Proc. IEEE/ION Position Location and Navigation Symp. (PLANS), pp. 1204-1211, 2010.
- J. W. Allen, C. Rose, J. Britt, and D. M. Bevly, "Intelligent multi-sensor measurements to enhance vehicle navigation and safety systems," in 2009 International Technical Meeting. Anaheim, California, 2009.

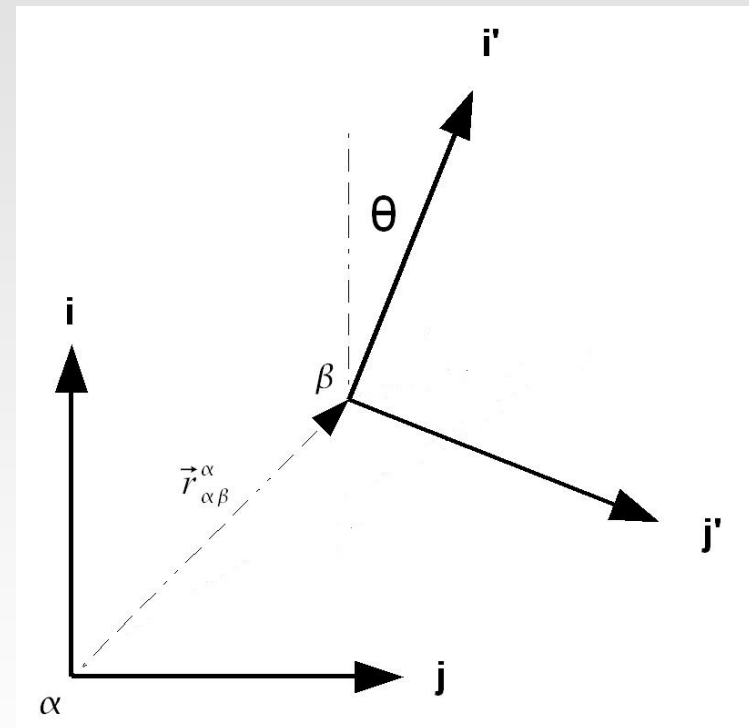


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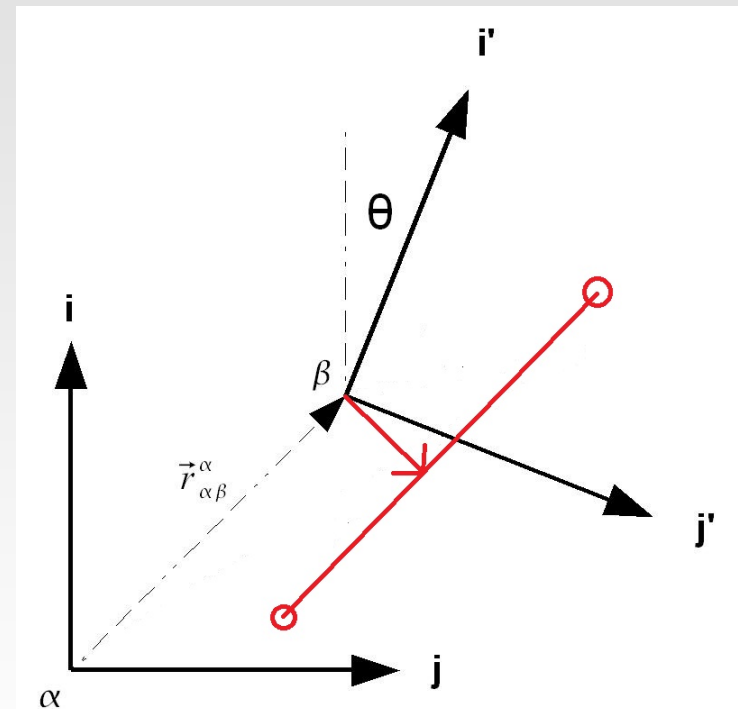
Background

- Typical navigation filter setup
 - Filter is based in a navigation coordinate frame
 - IMU measurements are given in the body coordinate frame and must be rotated into the navigation coordinate frame.
 - Update measurements are given in the navigation coordinate frame.
- Vision measurements are not given in the navigation coordinate frame.



Background

- If measurements are not given in the navigation coordinate frame, they can be rotated and translated to the navigation coordinate frame.
- This will not work for a lane position measurement

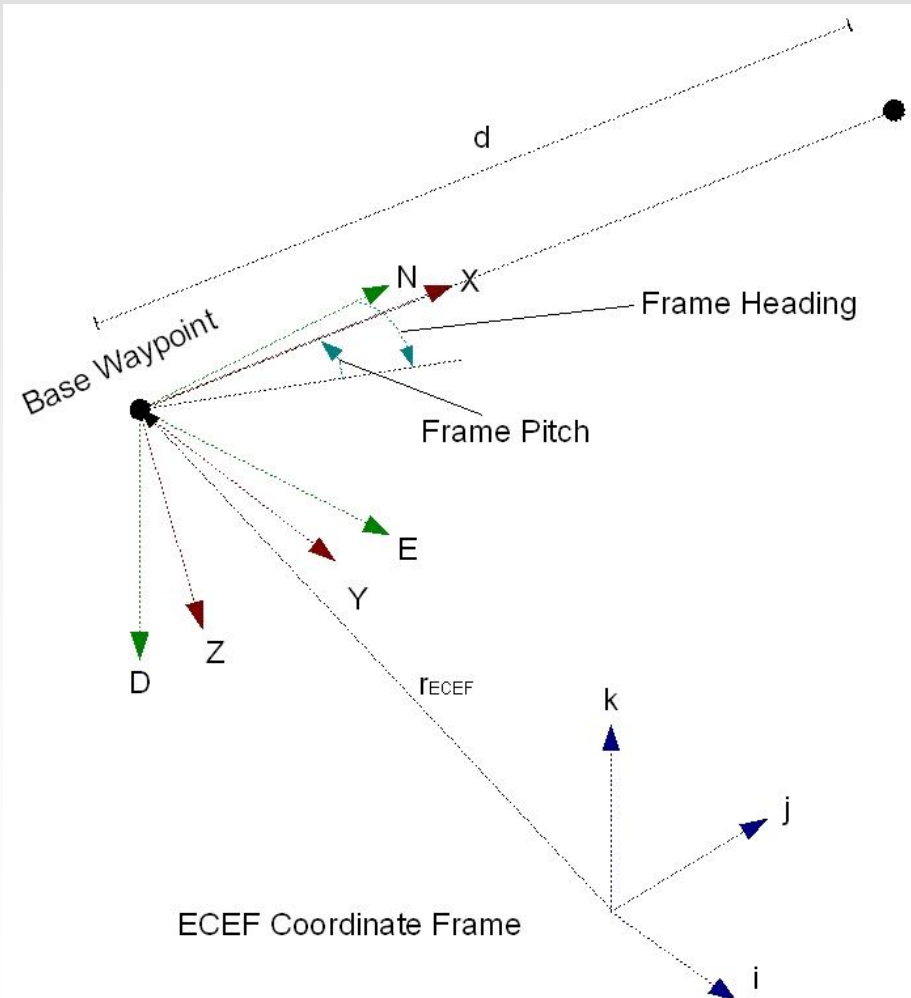


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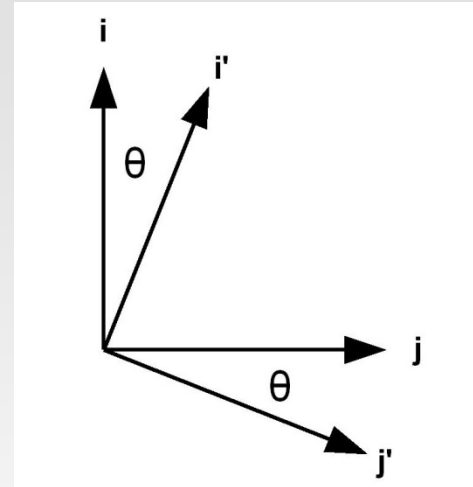
Background

- First approach was to construct a navigation filter with a navigation coordinate frame based on the waypoint map.
- Ideally, we would like to add lane position measurements to typical types of navigation filters.



Rotation 2D

- 2D rotations are based on one rotation
- Rotation is about an axis that is perpendicular to the 2D coordinate frame



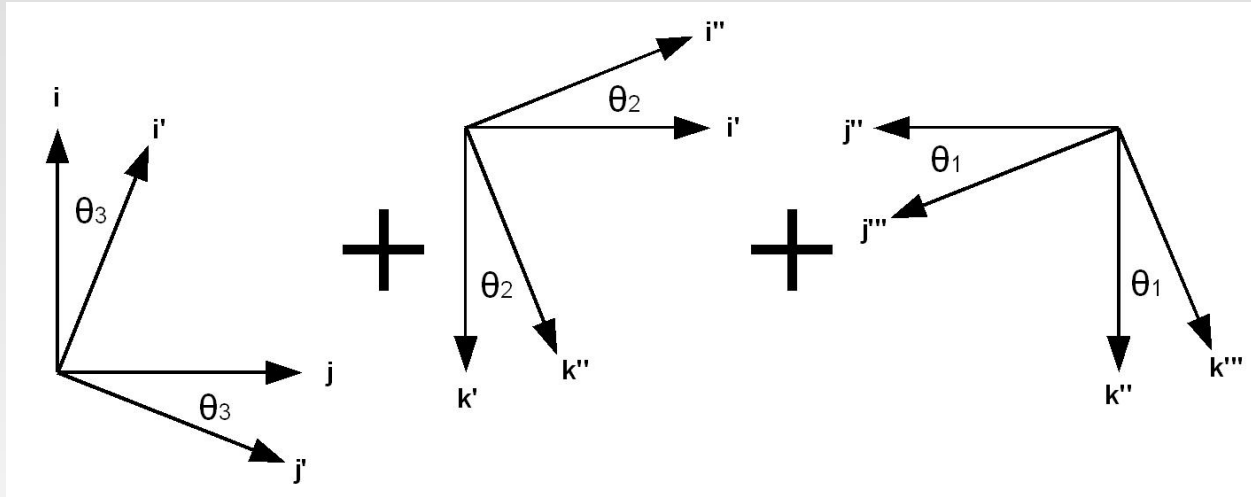
$$C_{(i,j)}^{(i',j')} = \begin{bmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{bmatrix}$$



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Rotation 3D



$$C_{(i,j)}^{(i''',j''')} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_1 & s_1 \\ 0 & -s_1 & c_1 \end{bmatrix} \begin{bmatrix} c_2 & 0 & -s_2 \\ 0 & 1 & 0 \\ s_2 & 0 & c_2 \end{bmatrix} \begin{bmatrix} c_3 & s_3 & 0 \\ -s_3 & c_3 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} c_2 c_3 & c_2 s_3 & -s_2 \\ s_1 s_2 c_3 - c_1 s_3 & s_1 s_2 s_3 + c_1 c_3 & s_1 c_2 \\ c_1 s_2 c_3 + s_1 s_3 & c_1 s_2 s_3 - s_1 c_3 & c_1 c_2 \end{bmatrix}$$



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Rotation and Translation

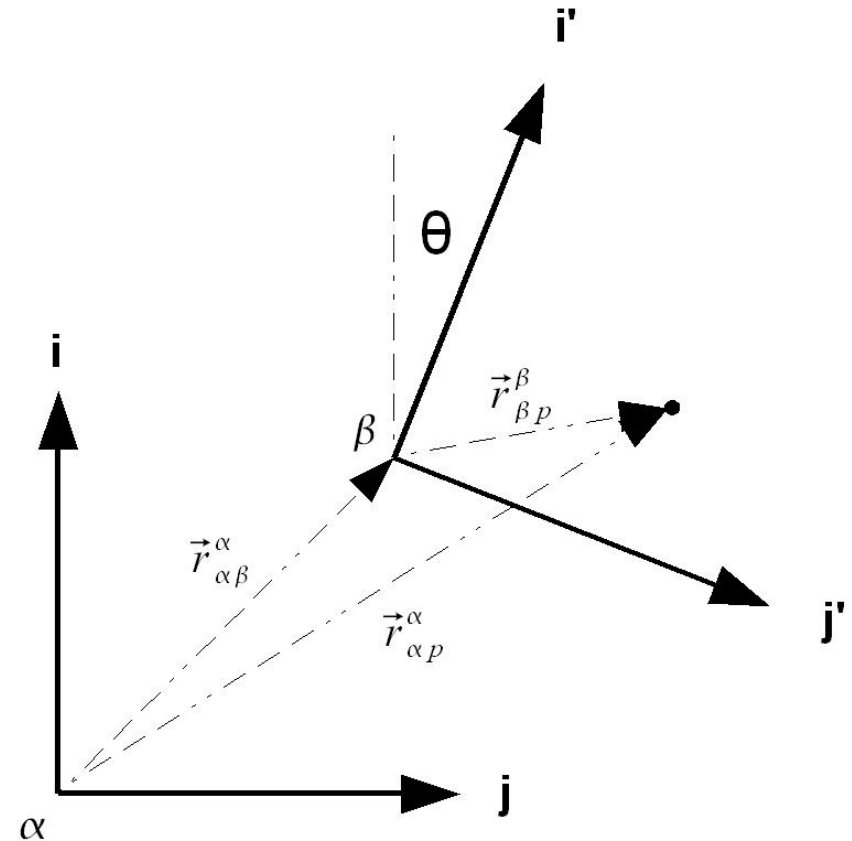
- Coordinates from 2 different coordinate frames can be mapped into each other.

$$\vec{r}_{\beta p}^{\beta} = C_{\alpha}^{\beta} [\vec{r}_{\alpha p}^{\alpha} - \vec{r}_{\alpha \beta}^{\alpha}]$$

$$\vec{r}_{\alpha p}^{\alpha} = C_{\beta}^{\alpha} \vec{r}_{\beta p}^{\beta} + \vec{r}_{\alpha \beta}^{\alpha}$$

$$\vec{v}^{\beta} = C_{\alpha}^{\beta} \vec{v}^{\alpha}$$

$$\vec{v}^{\alpha} = C_{\beta}^{\alpha} \vec{v}^{\beta}$$



Track Survey

- In order to use GPS to measure lane position, an accurate map of the lane must be constructed.
- For our project, we surveyed the NCAT test track in Opelika, AL.

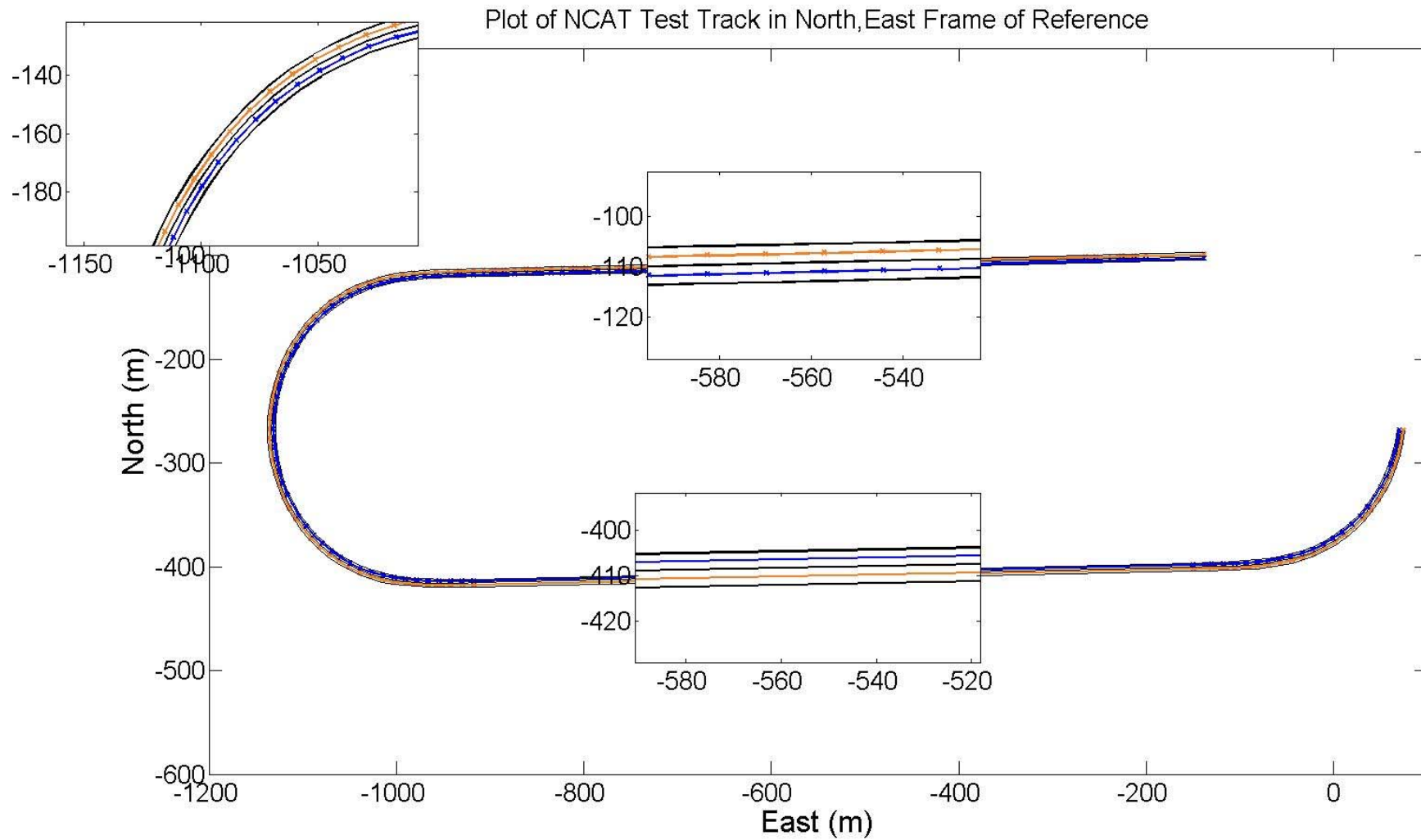


Google Earth

Track Survey



Track Map



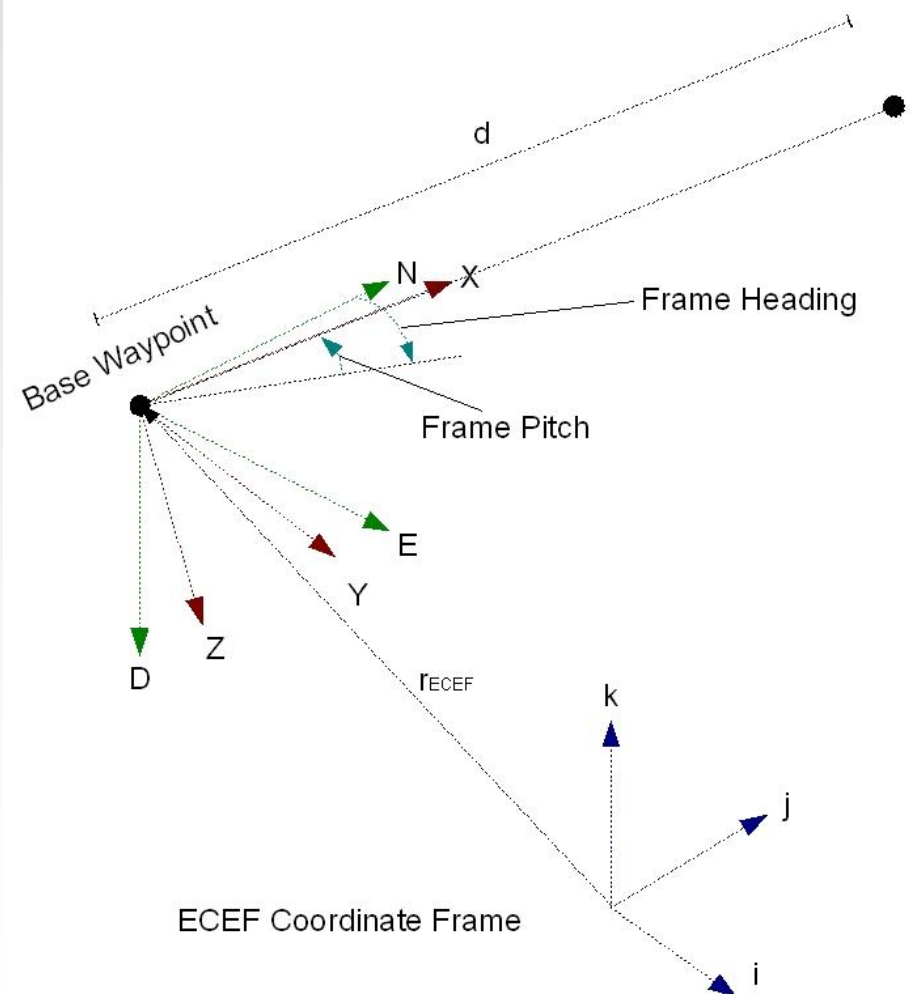
Track Map

- RTK GPS used to survey the track
- RTK provides a very accurate base line between base station and rover
- Survey should be saved as base-line vectors from a marked location in order to prevent global biasing



Track Map

- Along with waypoint positions, road attitude is needed
- Attitude represents rotation from the ECEF (navigation) coordinate frame to the Road (measurement) coordinate frame
- Road coordinate frame
 - X axis points in the from last waypoint passed to next waypoint
 - Y axis points right when facing direction of travel
 - Z axis points down with respect to the x-y plane



Track Map

- Can be thought of as 4 Euler rotations (longitude, latitude, road heading, and road pitch)
 - Longitude and Latitude can be determined from waypoint positions
 - Road heading and pitch can be determined by waypoint geometry.
- Wish to determine the 3 Euler angles that correspond to the 4 known rotations

$$\text{Map Database} = \begin{bmatrix} \vec{r}_{er,1}^e & \vec{\varphi}_1 & d_{r,1} \\ \vdots & \vdots & \vdots \\ \vec{r}_{er,m}^e & \vec{\varphi}_m & d_{r,m} \end{bmatrix}$$



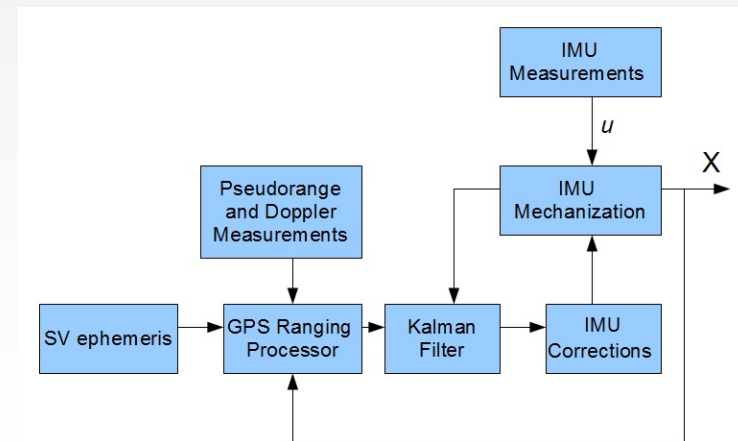
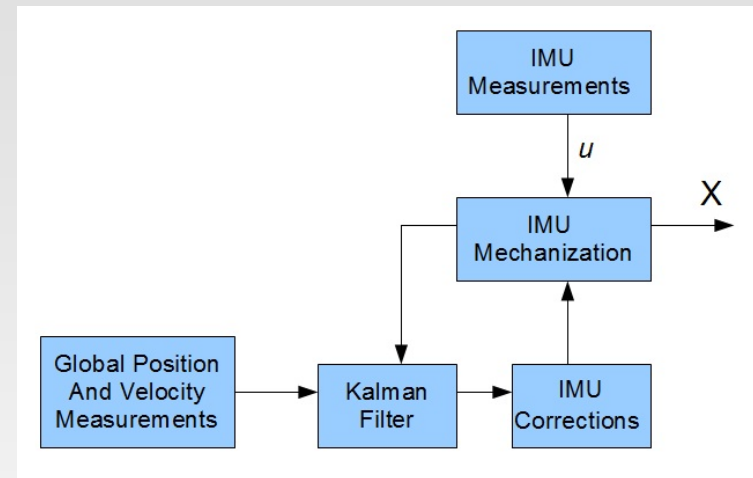
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6 DOF Filter Setup

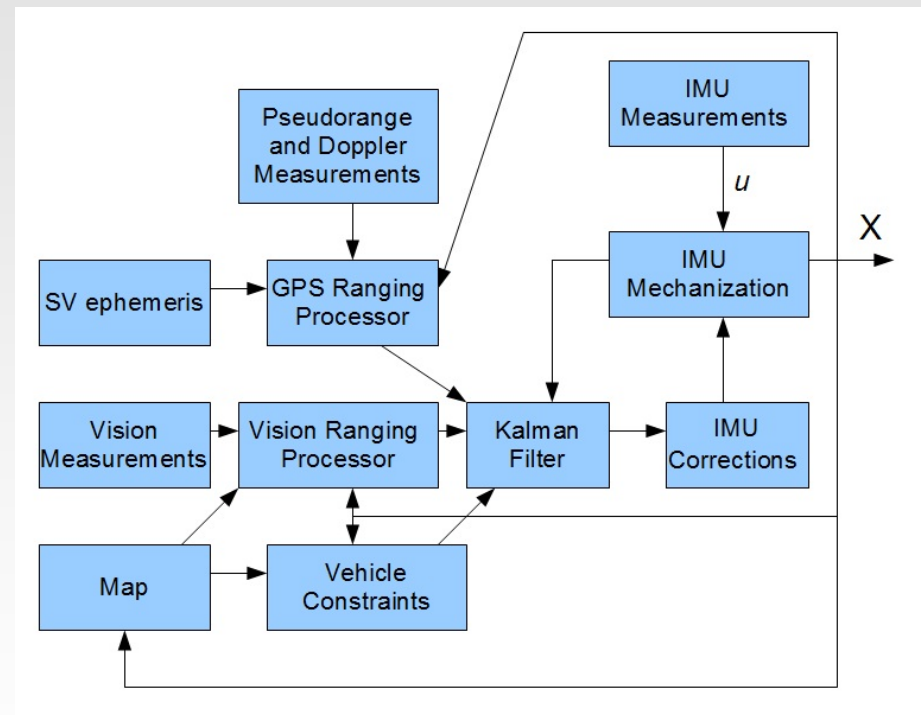
- States: position, velocity, attitude, accel/gyro biases, clock drift/bias
- Navigation coordinate frame is the global (ECEF) coordinate frame
- GPS measurements are given in the global coordinate frame

$$x = [r_{eb}^e \quad v_{eb}^e \quad \vec{a} \quad \vec{b}_f \quad \vec{b}_g \quad c\delta t \quad c\delta t]^T$$



6 DOF Filter Setup

- Adding lane map results in the ability to use measurements in the road coordinate frame
 - Vision is used to measure position in one axis
 - Height above the road is constant allowing measurement of position in another axis



Vision\Height Measurement Update

$$\text{Map Database} = \begin{bmatrix} \vec{r}_{er,1}^e & \vec{\varphi}_1 & d_{r,1} \\ \vdots & \vdots & \vdots \\ \vec{r}_{er,m}^e & \vec{\varphi}_m & d_{r,m} \end{bmatrix}$$

$$C_e^r = \begin{bmatrix} c_2 c_3 & c_2 s_3 & -s_2 \\ s_1 s_2 c_3 - c_1 s_3 & s_1 s_2 s_3 + c_1 c_3 & s_1 c_2 \\ c_1 s_2 c_3 + s_1 s_3 & c_1 s_2 s_3 - s_1 c_3 & c_1 c_2 \end{bmatrix}$$

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ \hat{z} \end{bmatrix} = C_e^r [\vec{r}_{eb}^e - \vec{r}_{er,i}^e]$$

$$h(x) = \begin{bmatrix} \hat{y} \\ \hat{h} \end{bmatrix} = \begin{bmatrix} C_e^r(2,1)(\vec{r}_{eb,1}^e - \vec{r}_{er,i,1}^e) + C_e^r(2,2)(\vec{r}_{eb,2}^e - \vec{r}_{er,i,2}^e) + C_e^r(2,3)(\vec{r}_{eb,3}^e - \vec{r}_{er,i,3}^e) \\ -C_e^r(3,1)(\vec{r}_{eb,1}^e - \vec{r}_{er,i,1}^e) - C_e^r(3,2)(\vec{r}_{eb,2}^e - \vec{r}_{er,i,2}^e) - C_e^r(3,3)(\vec{r}_{eb,3}^e - \vec{r}_{er,i,3}^e) \end{bmatrix}$$

$$e_1 = [C_e^r(2,1), C_e^r(2,2), C_e^r(2,3)]$$

$$e_2 = [-C_e^r(3,1), -C_e^r(3,2), -C_e^r(3,3)]$$

$$H(x) = \begin{bmatrix} e_1 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_2 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$



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Vision\Height Measurement Update

$$\text{Map Database} = \begin{bmatrix} \phi_{er,1} & \phi_1 & d_{r,1} \\ \vdots & \vdots & \vdots \\ \vec{r}_{er,m}^e & \vec{\phi}_m & d_{r,m} \end{bmatrix}$$

$$C_e^r = \begin{bmatrix} c_2 c_3 & c_2 s_3 & -s_2 \\ s_1 s_2 c_3 - c_1 s_3 & s_1 s_2 s_3 + c_1 c_3 & s_1 c_2 \\ c_1 s_2 c_3 + s_1 s_3 & c_1 s_2 s_3 - s_1 c_3 & c_1 c_2 \end{bmatrix}$$

$$\begin{bmatrix} \hat{x} \\ \hat{y} \\ \hat{z} \end{bmatrix} = C_e^r [\vec{r}_{eb}^e - \vec{r}_{er,i}^e]$$

$$h(x) = \begin{bmatrix} \hat{y} \\ \hat{h} \end{bmatrix} = \begin{bmatrix} C_e^r(2,1)(\vec{r}_{eb,1}^e - \vec{r}_{er,i,1}^e) + C_e^r(2,2)(\vec{r}_{eb,2}^e - \vec{r}_{er,i,2}^e) + C_e^r(2,3)(\vec{r}_{eb,3}^e - \vec{r}_{er,i,3}^e) \\ -C_e^r(3,1)(\vec{r}_{eb,1}^e - \vec{r}_{er,i,1}^e) - C_e^r(3,2)(\vec{r}_{eb,2}^e - \vec{r}_{er,i,2}^e) - C_e^r(3,3)(\vec{r}_{eb,3}^e - \vec{r}_{er,i,3}^e) \end{bmatrix}$$

$$e_1 = [C_e^r(2,1), C_e^r(2,2), C_e^r(2,3)]$$

$$e_2 = [-C_e^r(3,1), -C_e^r(3,2), -C_e^r(3,3)]$$

$$H(x) = \begin{bmatrix} e_1 & 0 & 0 & 0 & 0 & 0 & 0 \\ e_2 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

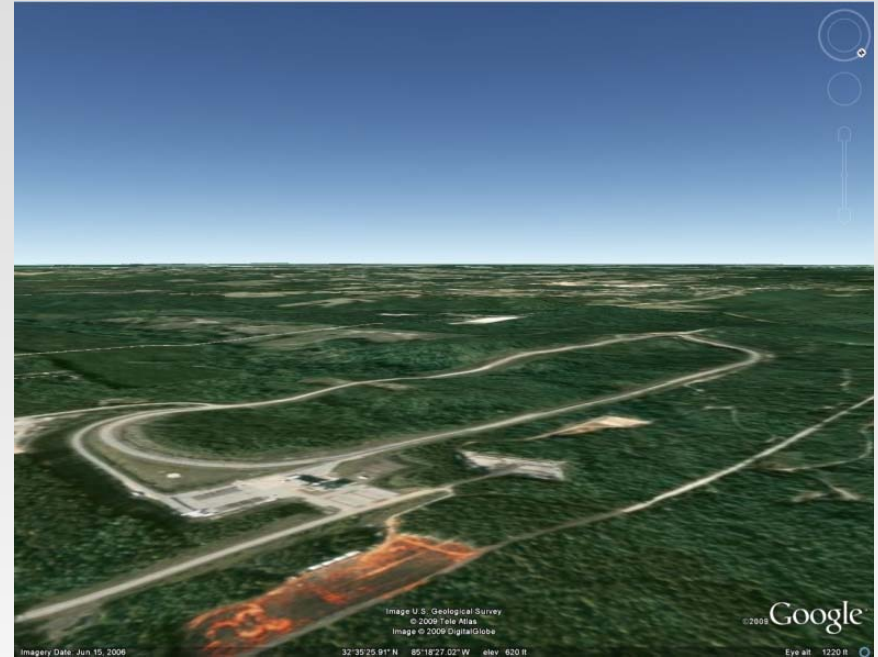


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Test Setup

- All test was done at the Nation Center for Asphalt Testing (NCAT) test track in Opelika, AL
 - 2 Lanes
 - 1.8 mile oval
 - 8 degrees of bank in the turns

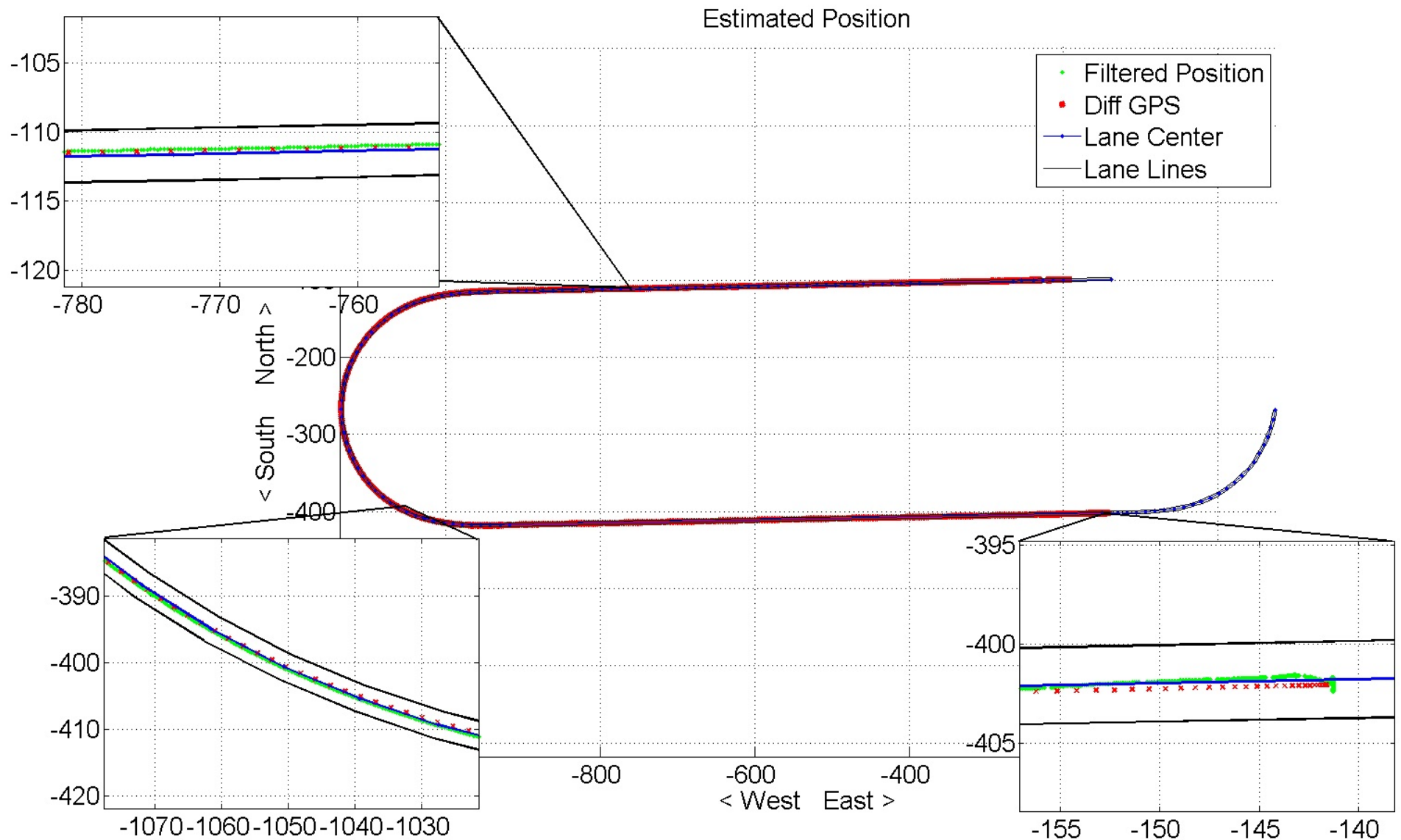


Test Setup

- Results obtained by post processing real data.
- All data was collected at the NCAT test track
- Equipment Used:
 - Septentrio GPS receiver
 - Crossbow 440 IMU
 - IBEO ALASCA XT laser scanner
 - Logitech QuickCam Pro 9000

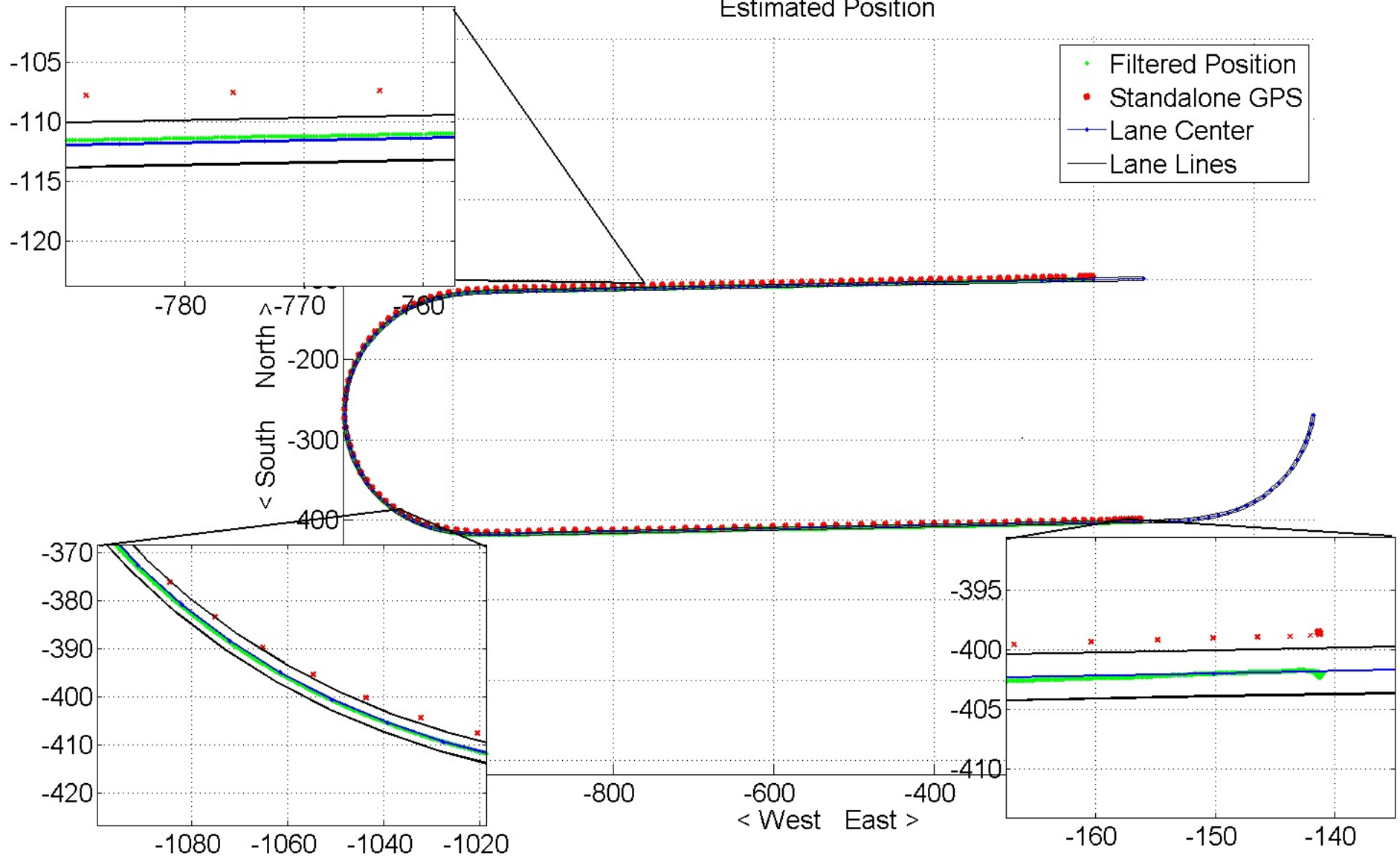


Results



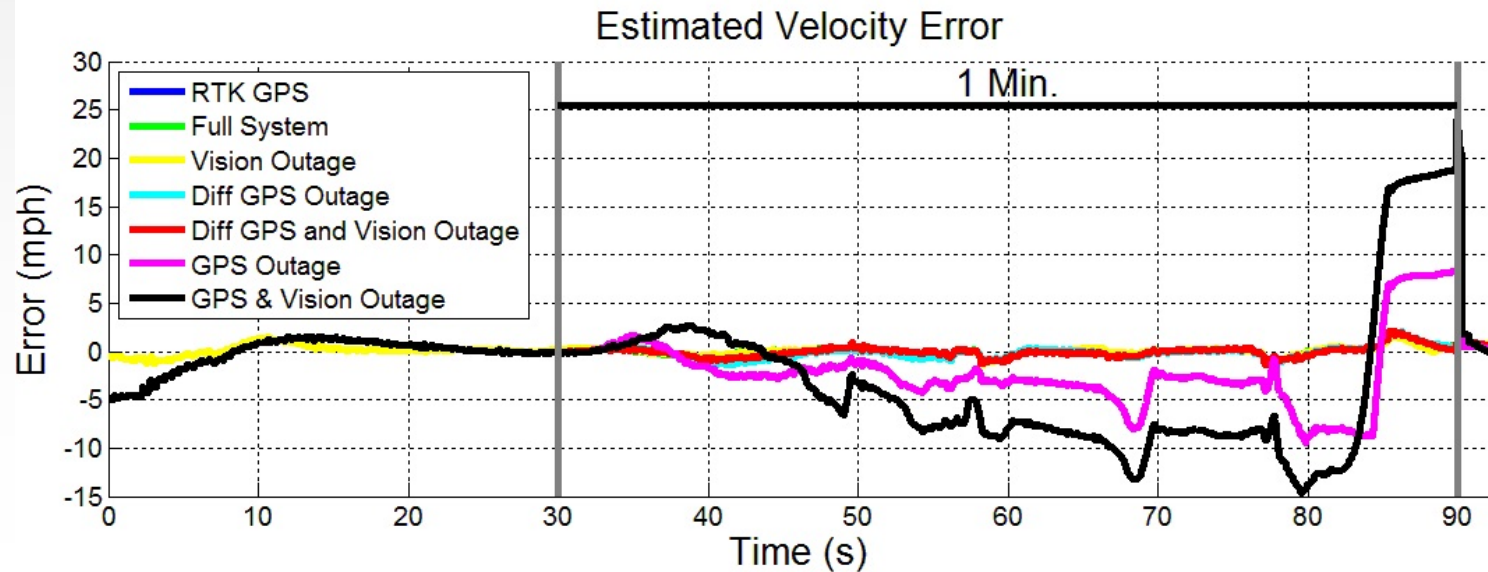
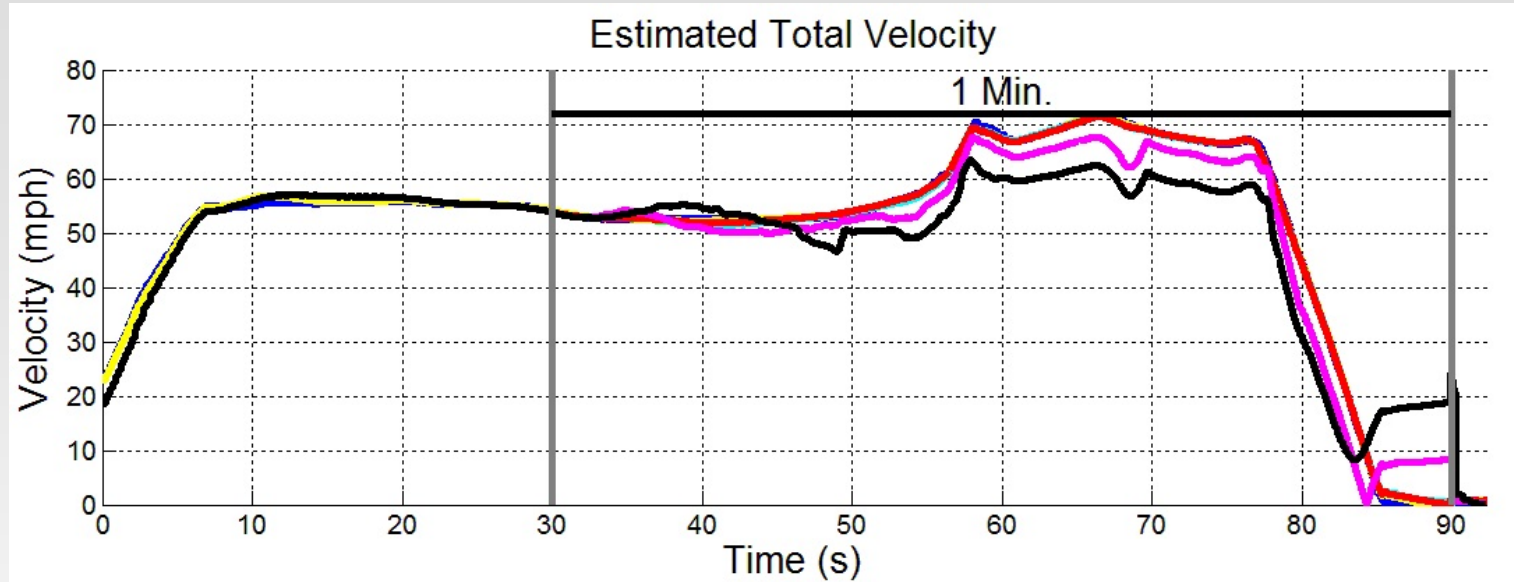
Results

Estimated Position

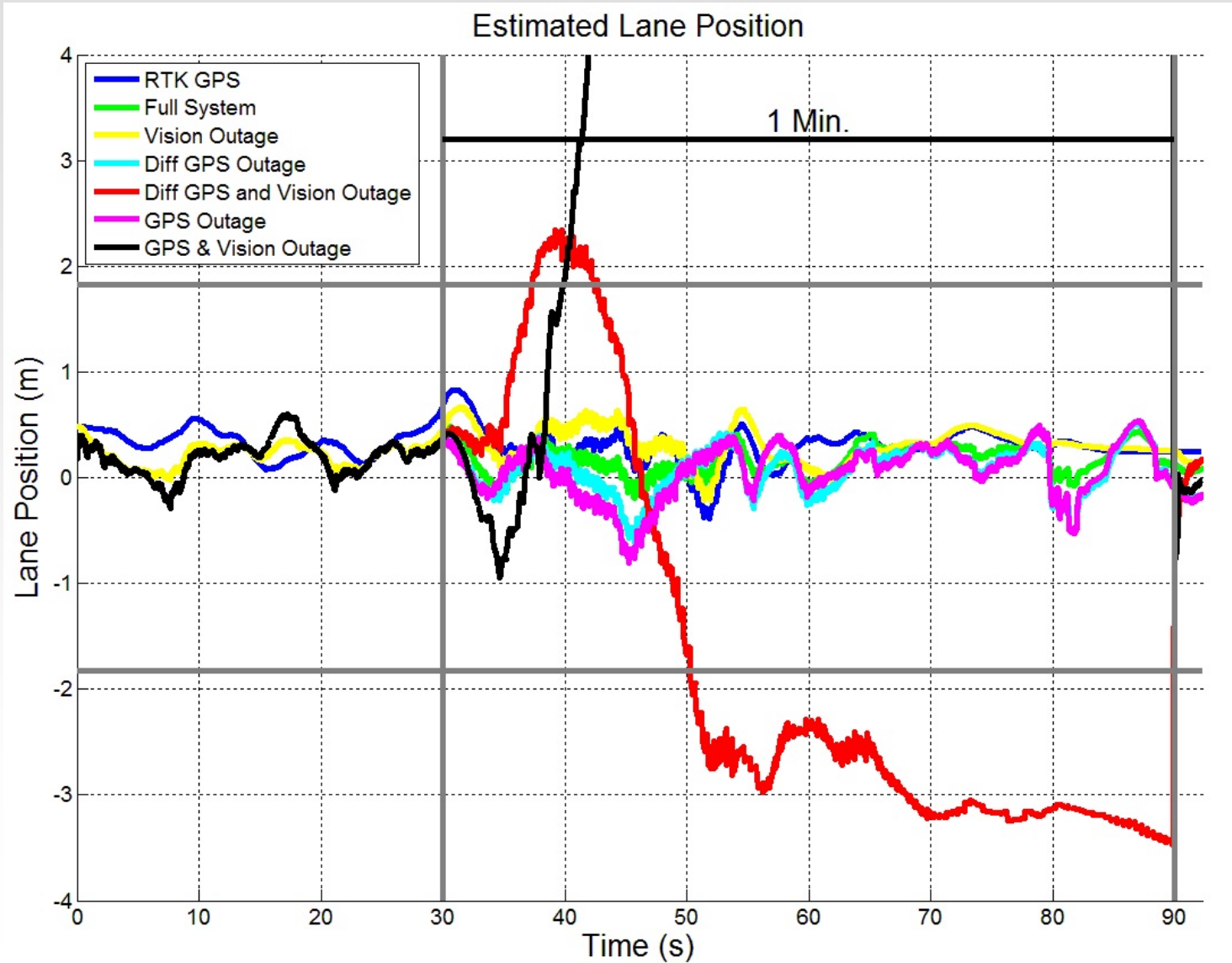




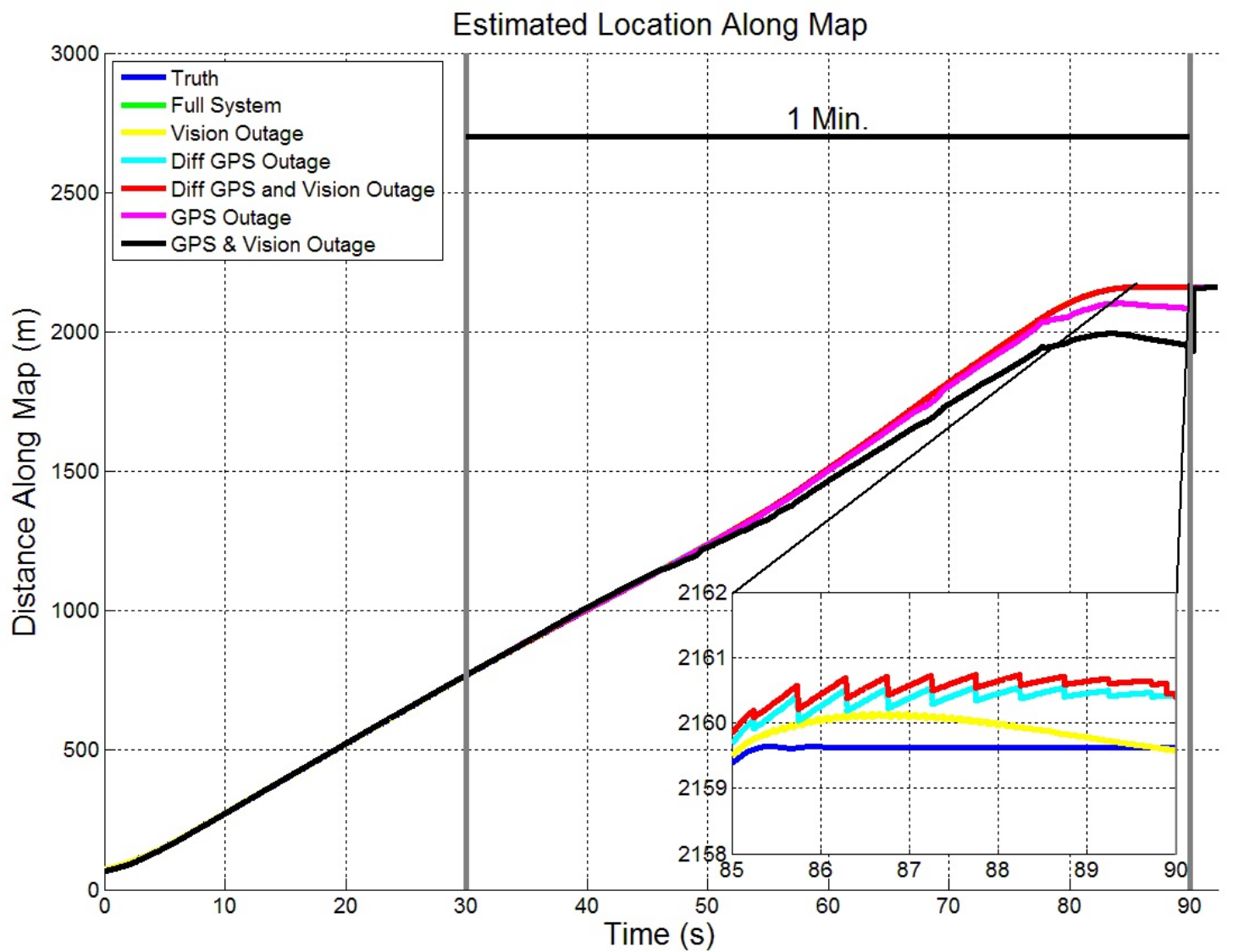
Results



Results

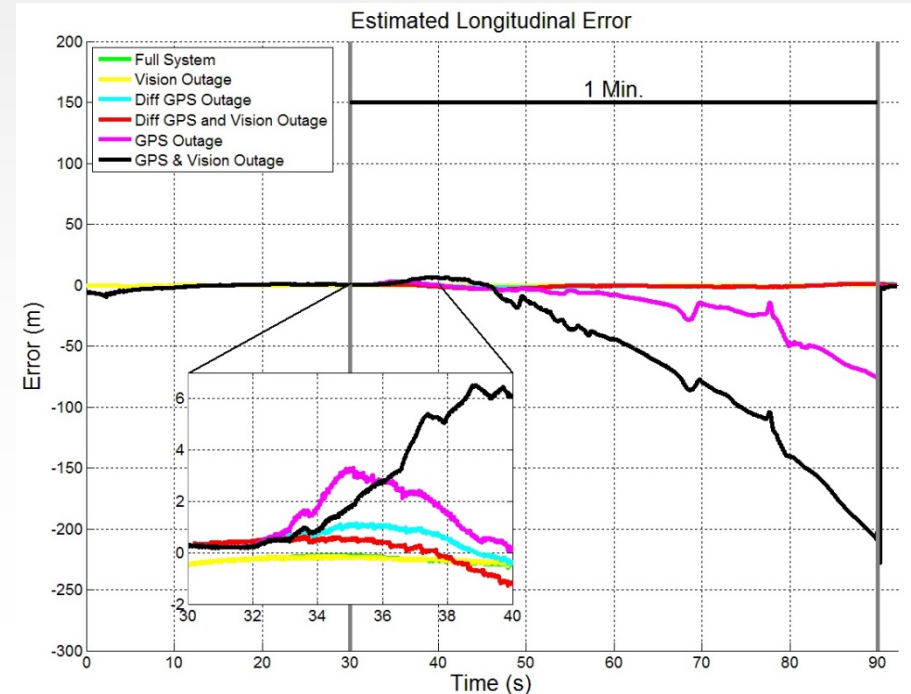
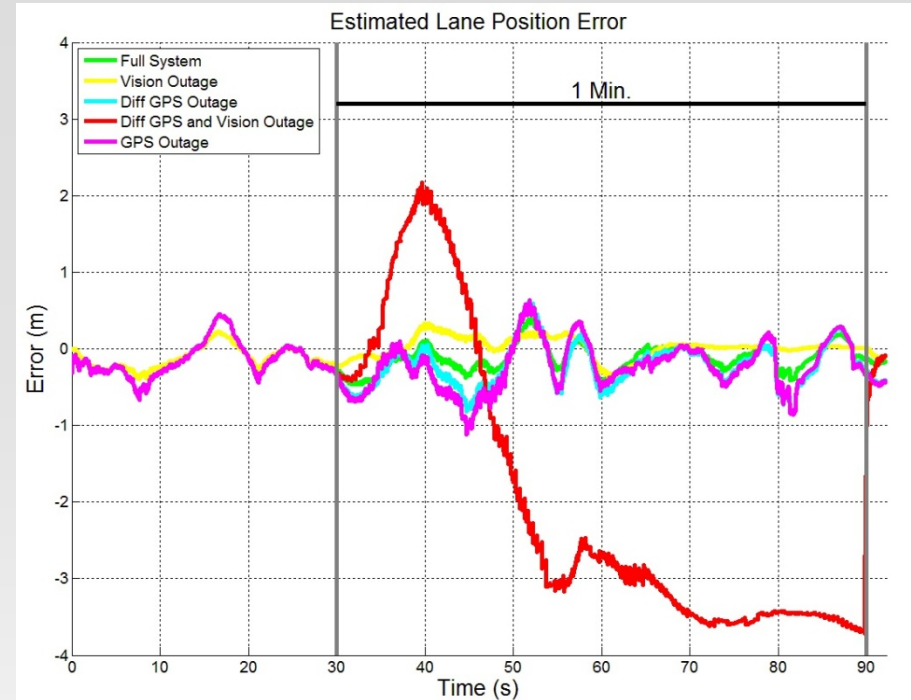


Results



Results

- Availability of differential GPS or vision measurements will result in lane level accuracy.
 - Standalone GPS can not achieve lane level position without the aid of vision
- Longitudinal position remains accurate as long as GPS is available.
 - Vision can be used to maintain lane position with no GPS, however, this will result in longitudinal position drift



Observability Analysis

- 11 States
- These equation assume a steady state attitude
- G =gravity vector expressed in navigation coordinate frame
- u =IMU input
 - u_1 - u_3 =accelerometer inputs

states

EOM

$$X = \begin{bmatrix} x \\ y \\ z \\ \dot{x} \\ \dot{y} \\ \dot{z} \\ b_{ax} \\ b_{ay} \\ b_{az} \\ ct_u \\ \dot{ct}_u \end{bmatrix} = \begin{bmatrix} X_1 \\ X_2 \\ X_3 \\ X_4 \\ X_5 \\ X_6 \\ X_7 \\ X_8 \\ X_9 \\ X_{10} \\ X_{11} \end{bmatrix}$$

$$\dot{X}_{11 \times 1} = \begin{bmatrix} X_{4:6} \\ C_{\text{Body}}^{\text{Nav}} (u_{1:3} - X_{7:9}) - G - \Omega \\ 0_{1 \times 3} \\ X_{11} \\ 0 \end{bmatrix}$$



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Closely Coupled (4 Observations)

- rank(OBS)=11 if the unit vector to each SV is independent
- Requires at least 4 observations to be fully observable.

$$C = \begin{bmatrix} a_1 & b_1 & c_1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & a_1 & b_1 & c_1 & 0 & 0 & 0 & 0 & 1 \\ a_2 & b_2 & c_2 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & a_2 & b_2 & c_2 & 0 & 0 & 0 & 0 & 1 \\ a_3 & b_3 & c_3 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & a_3 & b_3 & c_3 & 0 & 0 & 0 & 0 & 1 \\ a_4 & b_4 & c_4 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & a_4 & b_4 & c_4 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} O_{3 \times 3} & I_{3 \times 3} & O_{3 \times 3} & O_{3 \times 1} & O_{3 \times 1} \\ O_{3 \times 3} & O_{3 \times 3} & -C_{BODY}^{NAV} & O_{3 \times 1} & O_{3 \times 1} \\ O_{3 \times 3} & O_{3 \times 3} & O_{3 \times 3} & O_{3 \times 1} & O_{3 \times 1} \\ O_{1 \times 3} & O_{1 \times 3} & O_{1 \times 3} & 1 & 0 \\ O_{1 \times 3} & O_{1 \times 3} & O_{1 \times 3} & 0 & 0 \end{bmatrix}$$

unit vector to sv1=[a₁ b₁ c₁]
 unit vector to sv2=[a₂ b₂ c₂]
 unit vector to sv3=[a₃ b₃ c₃]
 unit vector to sv4=[a₄ b₄ c₄]

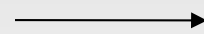
$$OBS = \begin{bmatrix} C \\ CA \\ CA^2 \\ \dots \\ CA^{13} \end{bmatrix}$$



H Tightly Coupled (2 Observations)

$$H = \begin{bmatrix} a_1 & b_1 & c_1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & a_1 & b_1 & c_1 & 0 & 0 & 0 & 0 & 0 & 0 & -1 \\ a_2 & b_2 & c_2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & a_2 & b_2 & c_2 & 0 & 0 & 0 & 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

rank(obs)=8



$$C = \begin{bmatrix} a_1 & b_1 & c_1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & a_1 & b_1 & c_1 & 0 & 0 & 0 & 0 & 1 \\ a_2 & b_2 & c_2 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & a_2 & b_2 & c_2 & 0 & 0 & 0 & 0 & 1 \\ a_3 & b_3 & c_3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ a_4 & b_4 & c_4 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

rank(obs)=11

$$OBS = \begin{bmatrix} C \\ CA \\ CA^2 \\ \dots \\ CA^{13} \end{bmatrix}$$

Observability Analysis (2 Observations)

	Elevation	Azimuth
SV1	60	90
SV2	30	-90

$$H = \begin{bmatrix} 0 & .5 & -.866 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & .5 & -.866 & 0 & 0 & 0 & 0 & 1 \\ 0 & -.866 & -.5 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & -.866 & -.5 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

- No x axis position or x axis velocity information is provided by the GPS observations. This causes a loss of observability.

$$OBS = \begin{bmatrix} C \\ CA \\ CA^2 \\ \dots \\ CA^{13} \end{bmatrix}$$

$$\text{rank}(obs)=10$$

Observability Analysis (2 Observations)

	Elevation	Azimuth
SV1	45	0
SV2	45	180

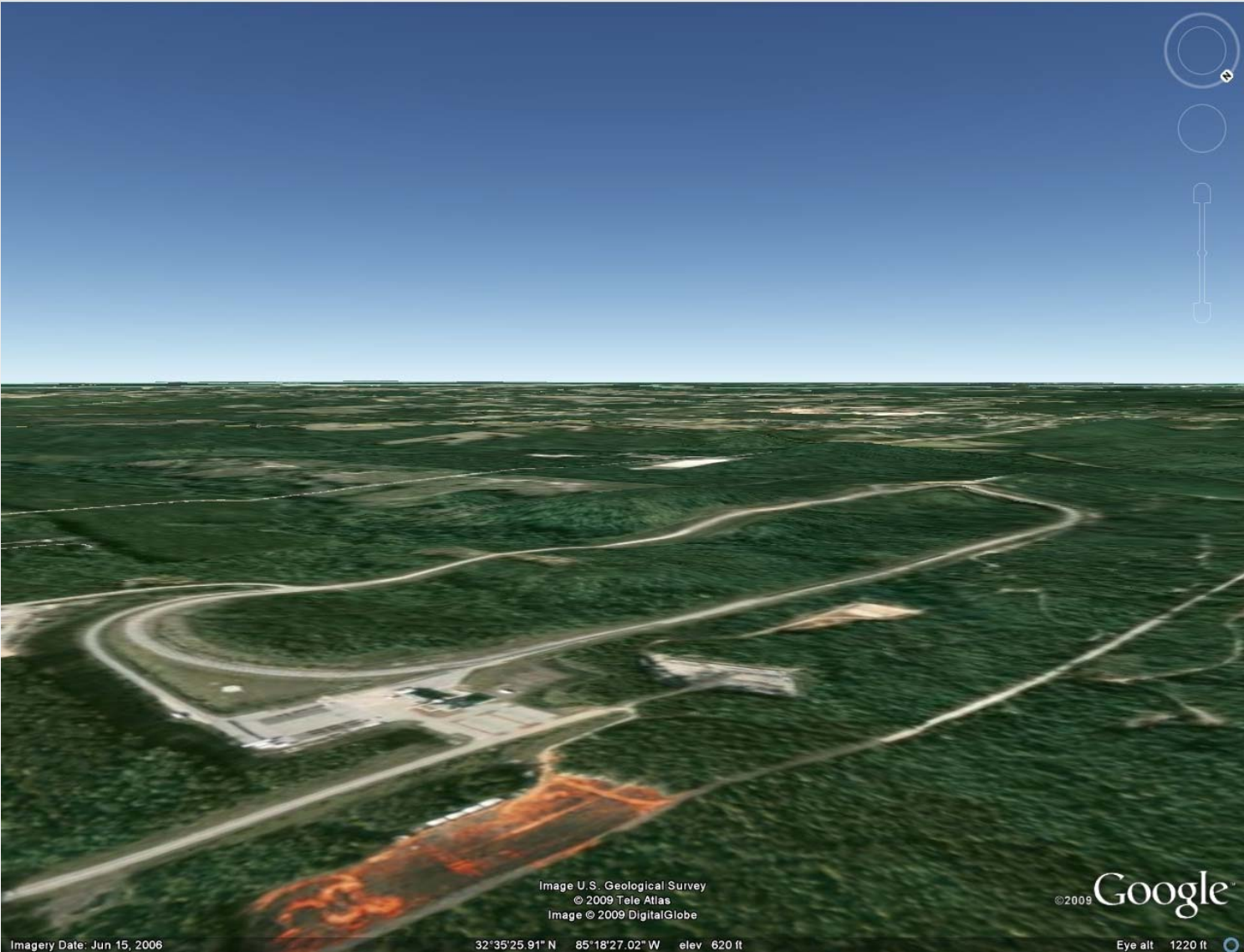
$$H = \begin{bmatrix} .707 & 0 & -.707 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & .707 & 0 & -.707 & 0 & 0 & 0 & 0 & 1 \\ -.707 & 0 & -.707 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -.707 & 0 & -.707 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

- No y axis position or y axis velocity information is provided by the GPS observations: however, the system is still observable because the vision measurements provide information in the y axis.

$$OBS = \begin{bmatrix} C \\ CA \\ CA^2 \\ \dots \\ CA^{13} \end{bmatrix}$$

$$\text{rank}(obs)=11$$

NCAT Test Track



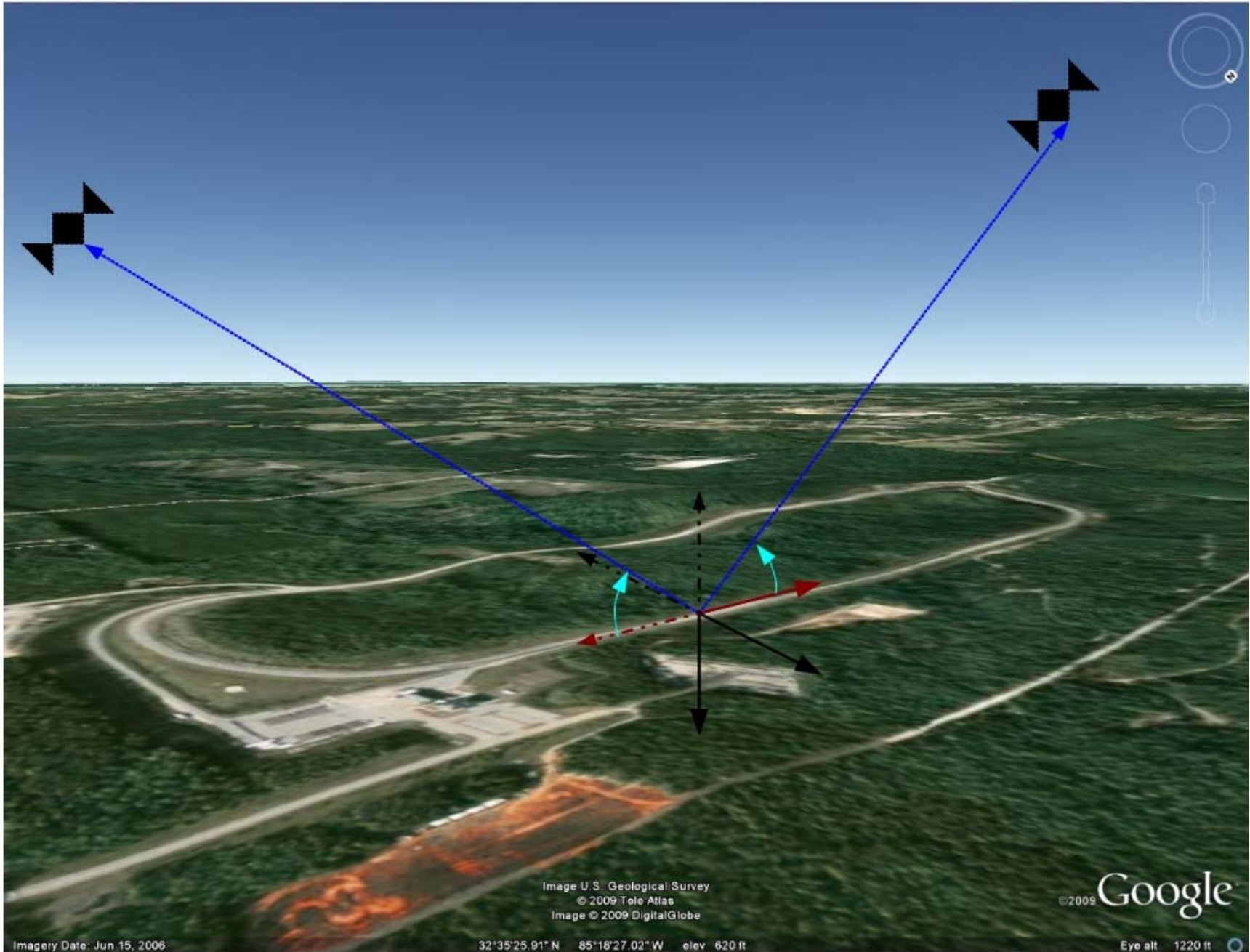


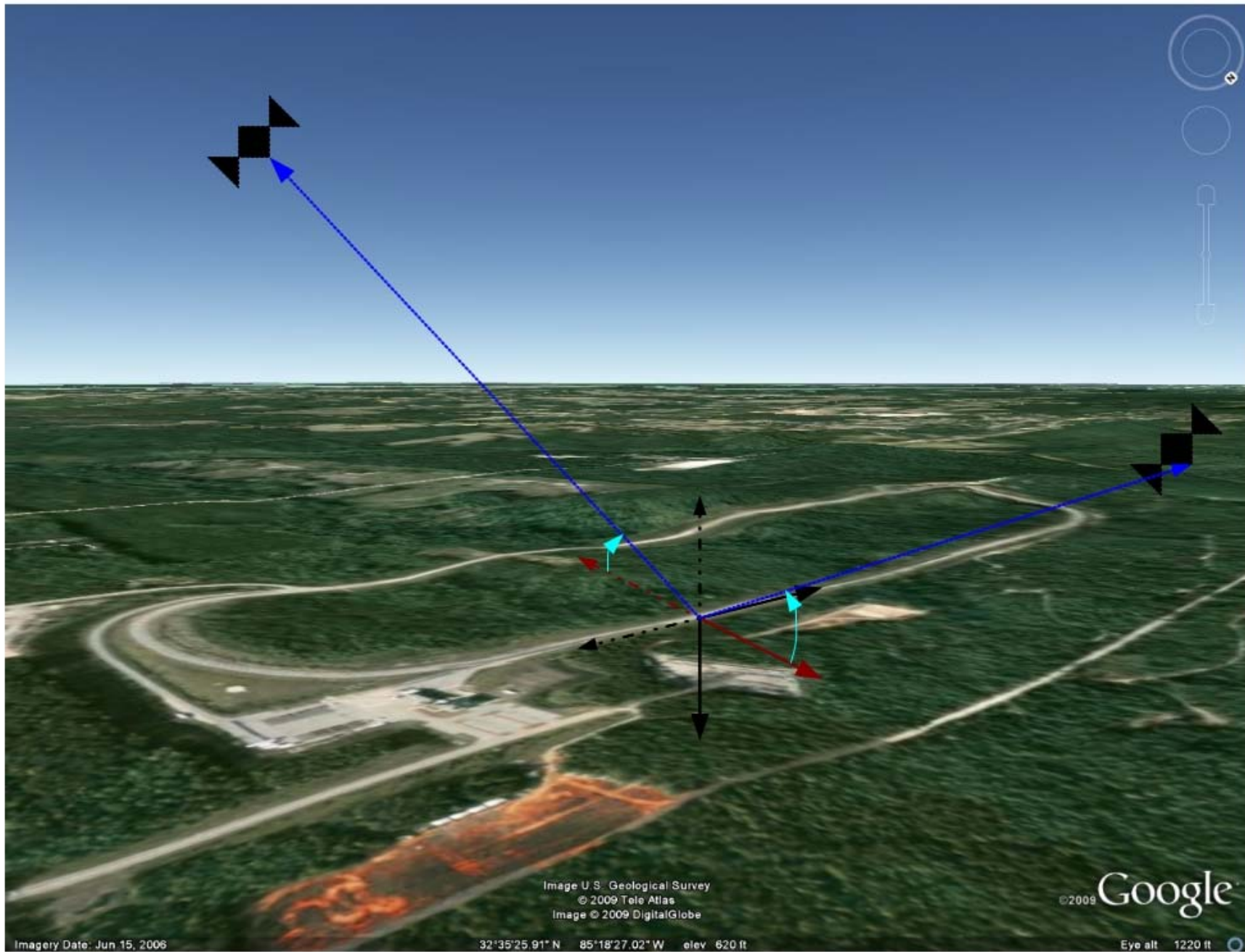
Image U.S. Geological Survey
© 2009 Tele Atlas
Image © 2009 DigitalGlobe

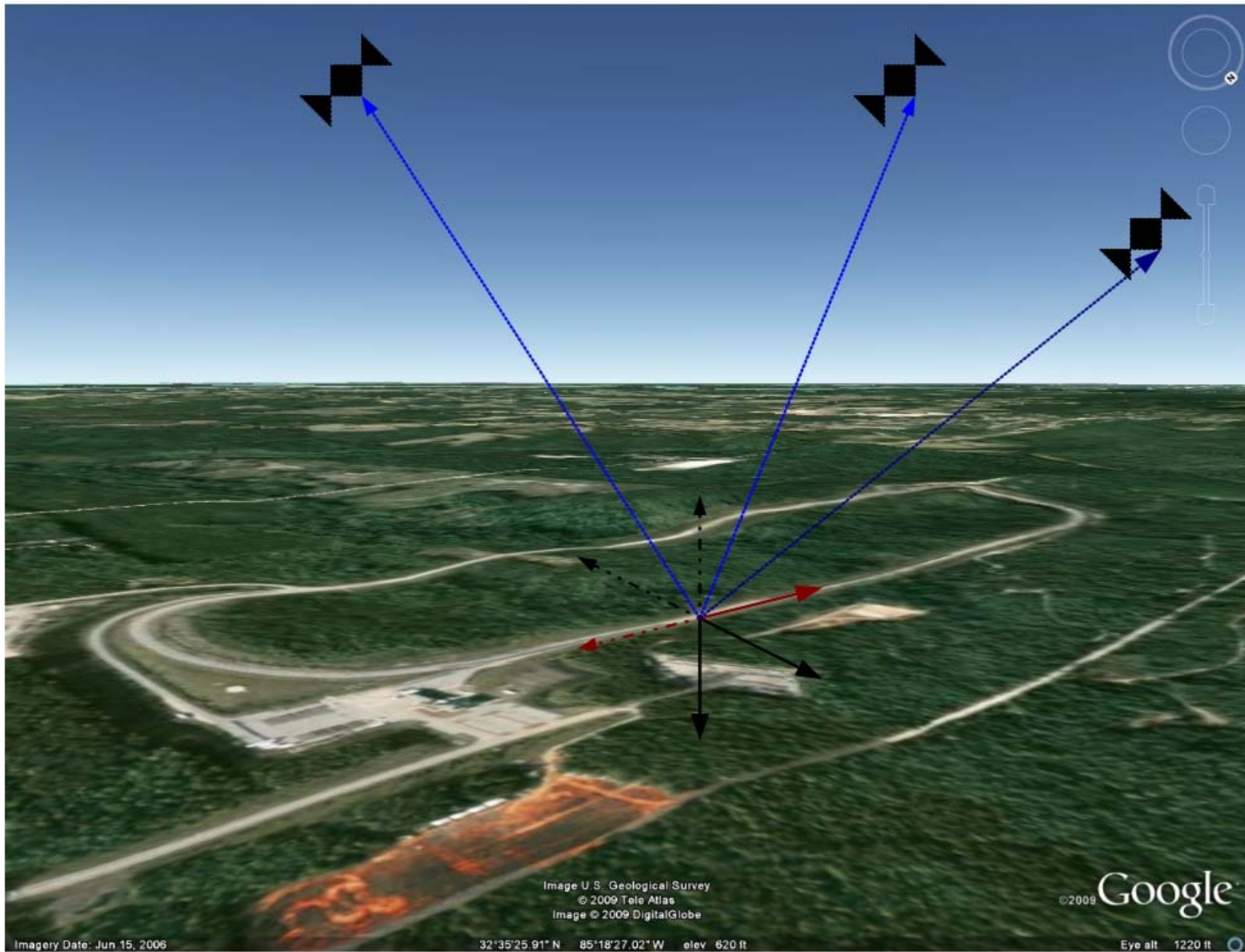
©2009 Google

Imagery Date: Jun 15, 2006

32°35'25.91" N 85°18'27.02" W elev. 620 ft

Eye alt. 1220 ft





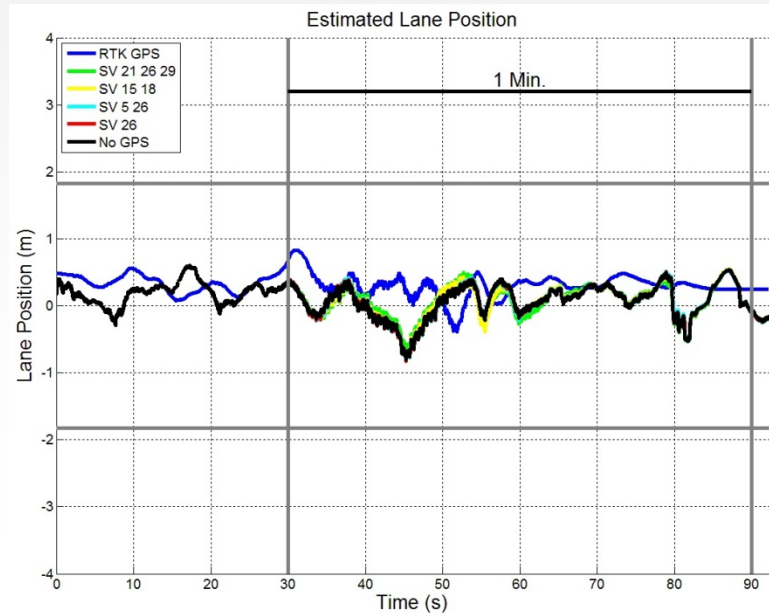
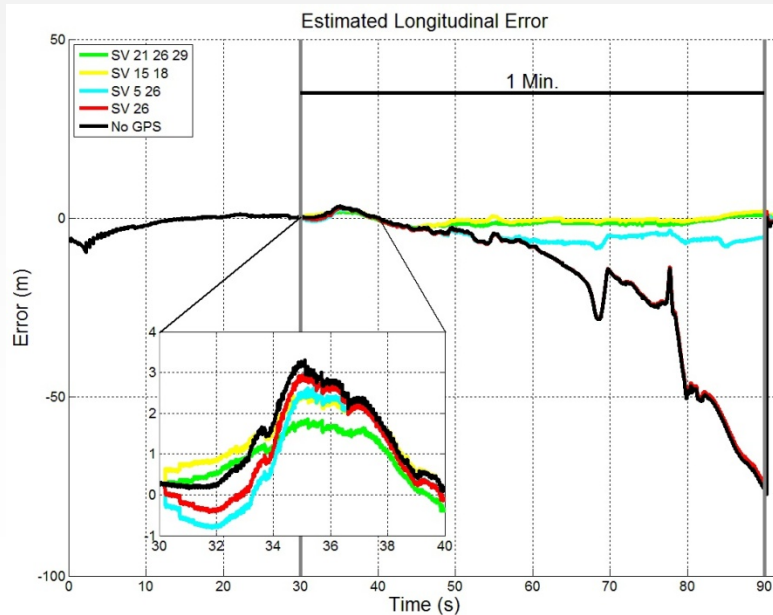
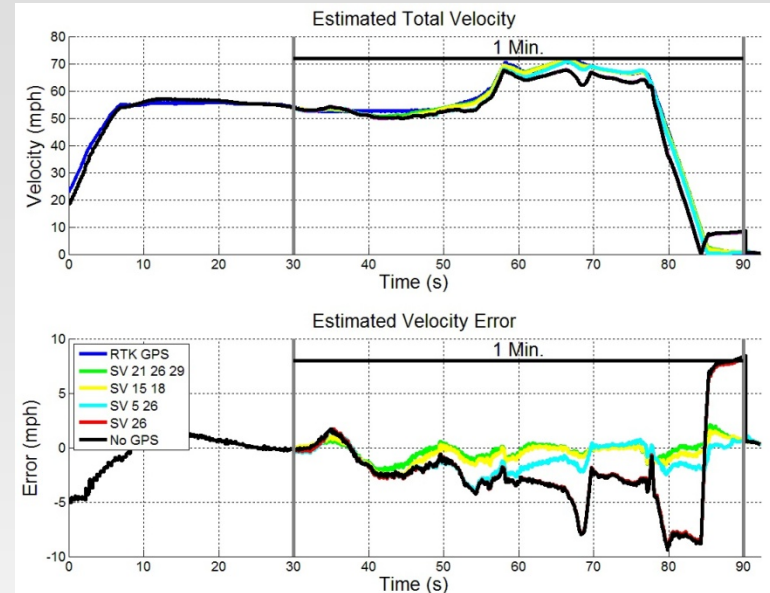
Results

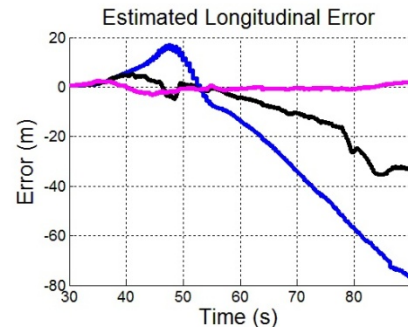
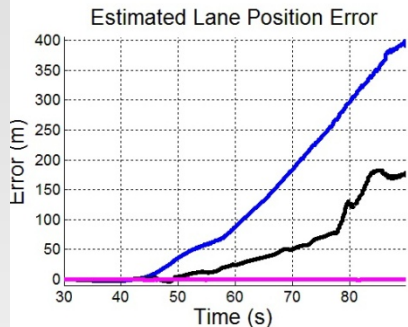
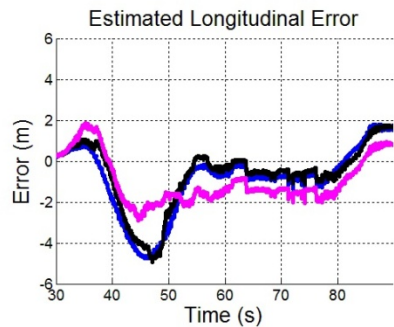
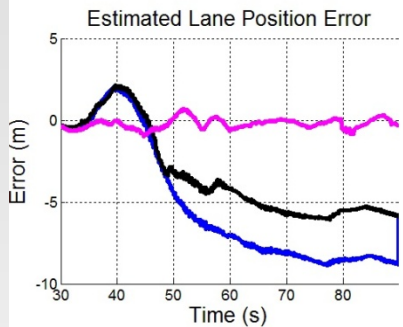
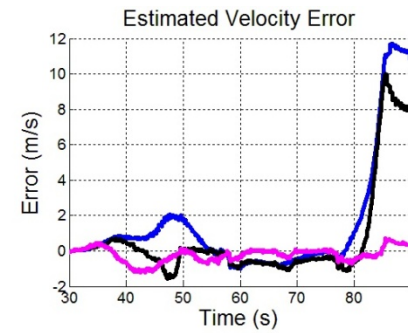
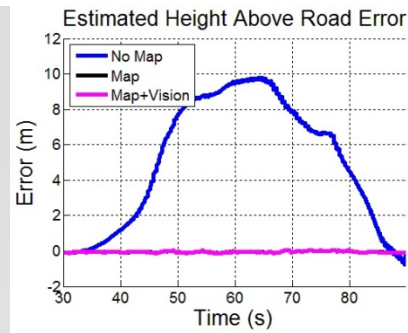
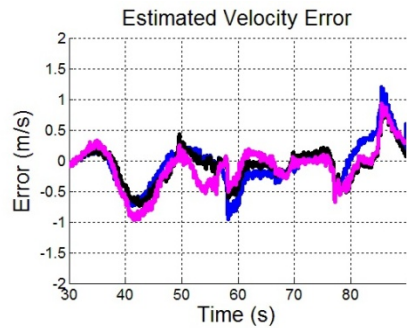
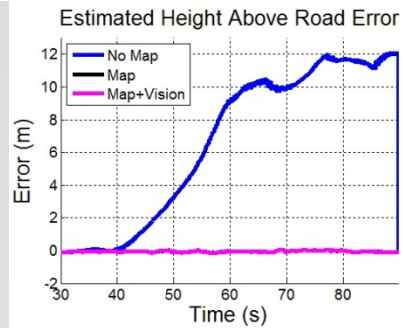
	Elevation	Azimuth
SV5	19	63
SV9	16	151
SV15	80	100
SV18	38	-80
SV21	52	-39
SV26	44	47
SV27	25	129
SV29	49	148



Results

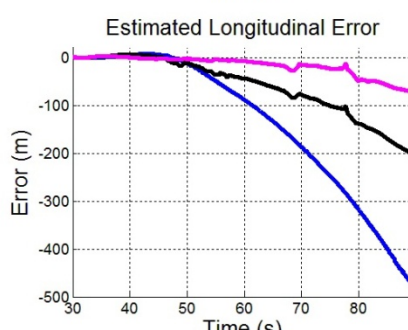
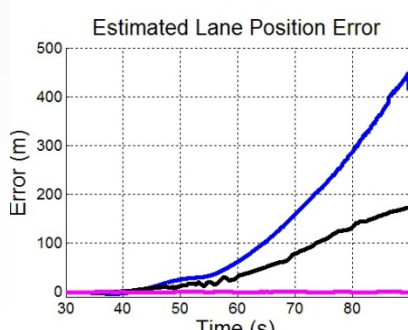
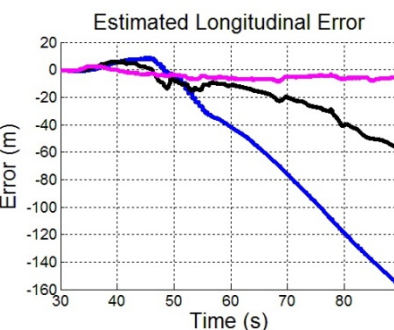
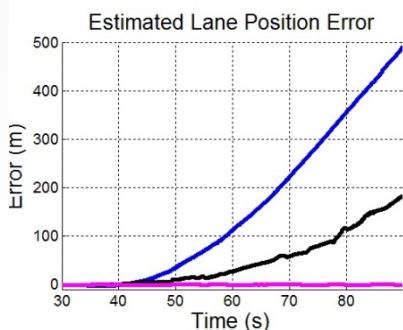
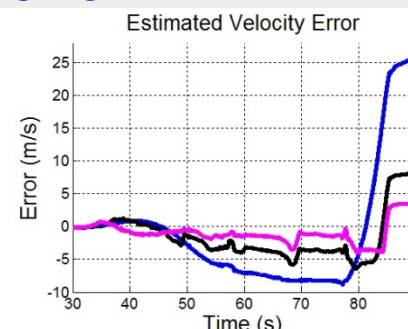
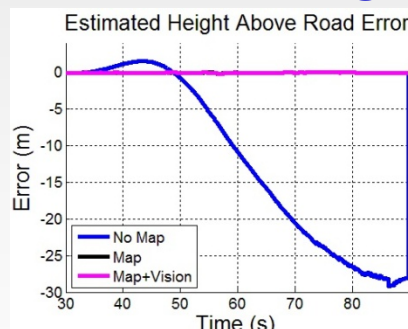
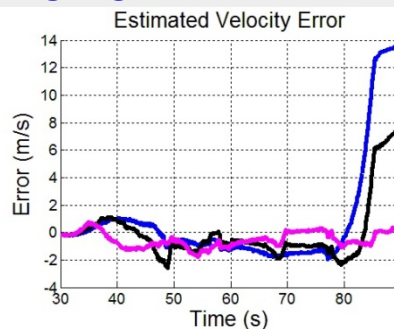
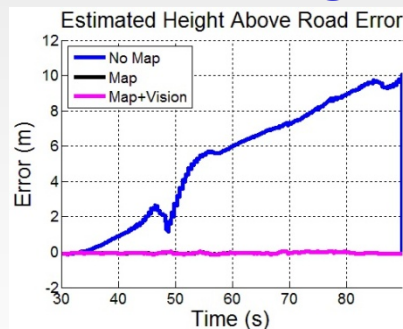
- Velocity error directly corresponds to number of observations available
- Using vision during satellite outages results in better overall velocity estimation
- There is no benefit when using only 1 GPS observation





SV 21 26 29

SV 15 18

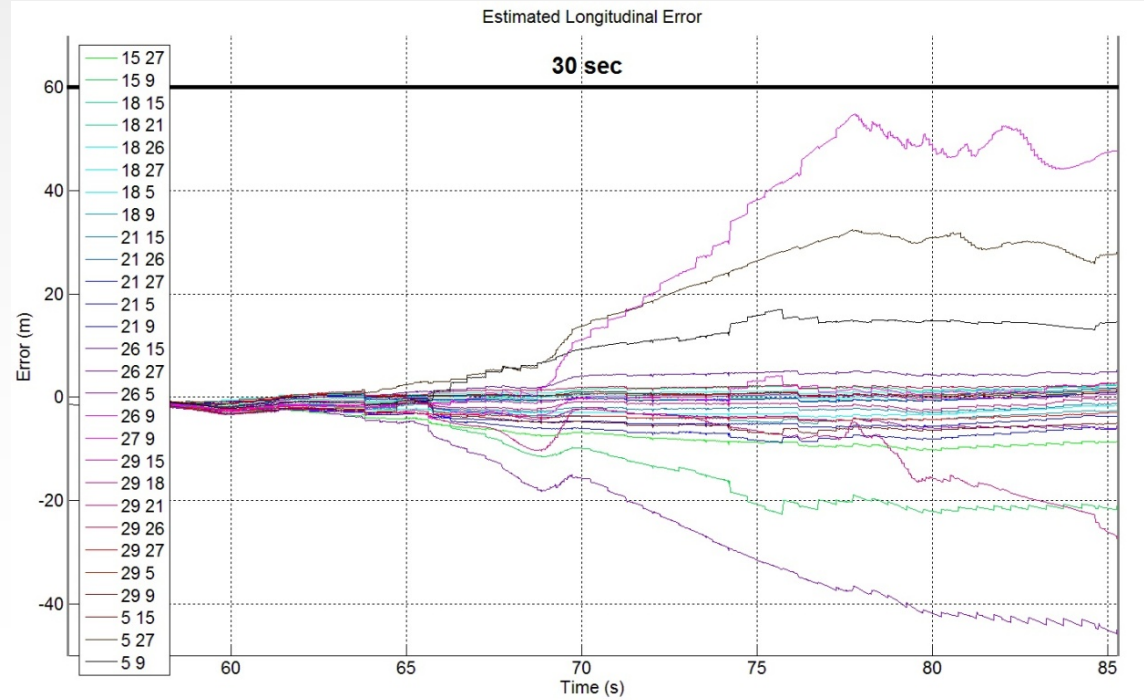
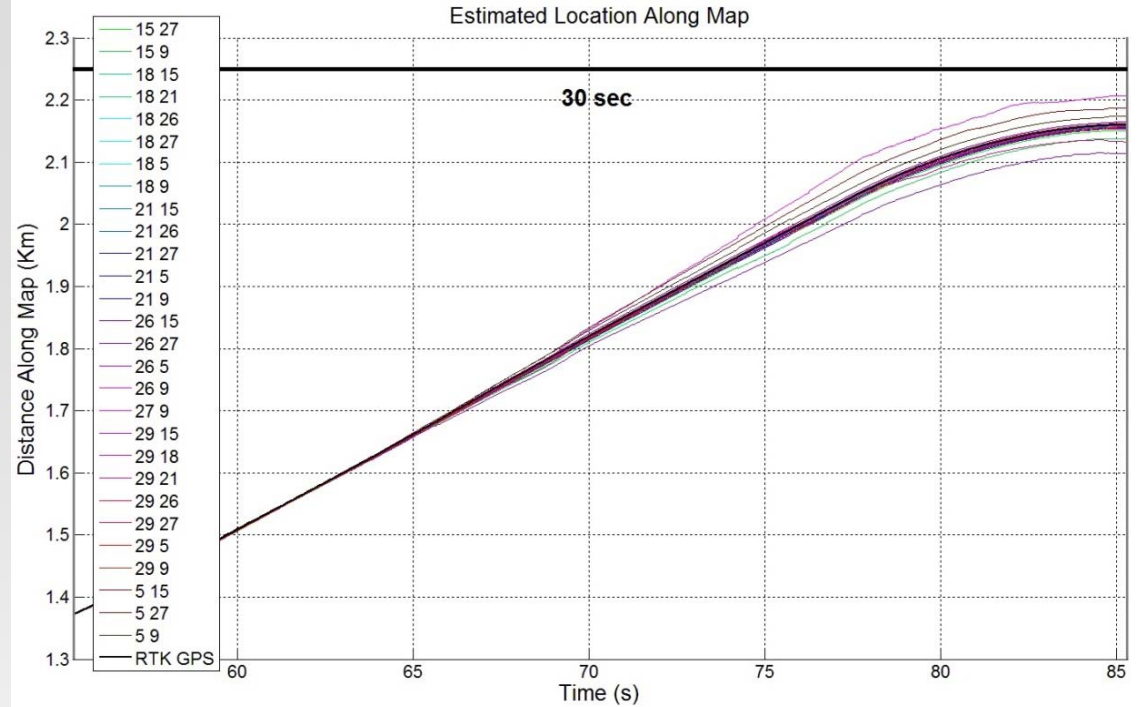


SV 5 26

SV 26

Results

	C2N
SV5	48
SV9	48
SV15	54
SV18	53
SV21	52
SV26	48
SV27	42
SV29	51



Conclusions

- It is possible to use measurements in a coordinate frame that is not aligned with the navigation coordinate frame.
- This technique can be applied to any situation where the measurement coordinate frame and navigation coordinate frame do not align.
- Using an accurate map along with vision based lane position measurements will improve global accuracy in 2 dimensions.
- It is possible to have a fully observable navigation filter only using 2 GPS satellites as long as supplemental measurements are provided. Using only 2 GPS satellites will result in more estimate error than using a full GPS satellite constellation.
- Effects of satellite geometry will increase as the number of GPS observations used decreases.



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Future Work

- Use multiple waypoint maps to create a filter that can track lane changes and track the current lane the vehicle resides
- Use DSRC ranging, visual odometry, and road signature maps to further improve robustness
- Develop maps that incorporate road bank
- Develop maps that are equation based instead of way-point based.
- Use of SLAM or other techniques simultaneous positioning and mapping.



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