

Inertial Sensors (MEMS Accelerometer Architectures) Continued

Force feedback accelerometers

All the previously discussed accelerometer architectures have been open loop. Next, we will discuss some closed loop (or force feedback) accelerometer architectures.

a. Limitations of open loop accelerometers

In the open-loop designs, the output signal = $f(\text{proof mass displacement})$. This results in some limitations:

1. For clamped multi-beam suspensions systems designs: the proof mass displacement is a nonlinear function of the applied acceleration, especially for large displacements.
2. Fluidic damping around the suspension system and proof mass adds additional nonlinear effects as the proof mass displaces.
3. With accelerometer sensitivity, S , high sensitivity = low bandwidth.

b. Closed loop accelerometers

A closed loop feedback controller is used to keep the proof mass in the same position over the measurable range of acceleration.

Any proof mass displacement is detected with piezoresistors or capacitively, and reduced to zero using one or more MEMS actuators (PPA, CDA, etc.).

Closed loop accelerometers have several advantages:

1. They avoid clamped beam and fluidic induced nonlinearities.
2. The sensitivity is set by the control loop and not by the mechanical bandwidth.
3. Additional features are possible, such as BIST, and temperature compensation.
4. They can have improved performance, such as a wider acceleration measurement range.

Closed loop accelerometers do have some disadvantages too:

1. Increased complexity (more things that can go wrong).
2. Added cost (more components, lower yield).

1) Analog closed-loop accelerometers

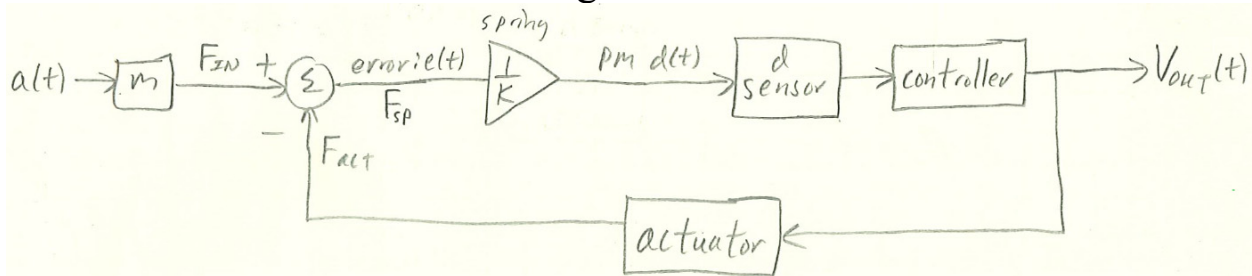
Similar to force feedback pressure sensors, we will use an actuator to produce a force equal in magnitude but opposite in direction to the inertial force affecting the proof mass. In the force feedback pressure sensor, it was a difference in pressure affecting the diaphragm that the actuator corrected for.

So to make this work, we need several components:

- (1) Sensor(s) to detect proof mass motion
- (2) Actuator(s) to move the proof mass back to its rest position

- (3) A closed loop controller (feedback network) to process the output of the sensor(s) and generate an appropriate drive signal to the actuator(s).

Consider this controller block diagram:



F_{IN} is the inertial force: $F_{IN} = ma$

F_{SP} is the spring force: $F_{SP} = kd$

F_{act} is the force produced by the actuator

F_{sp} is also the error signal, $e(t)$, which the controller attempts to make equal to zero.

The three boxes, d sensor, controller, and actuator, might be as simple as a gain, or as complex as a second order dynamic system.

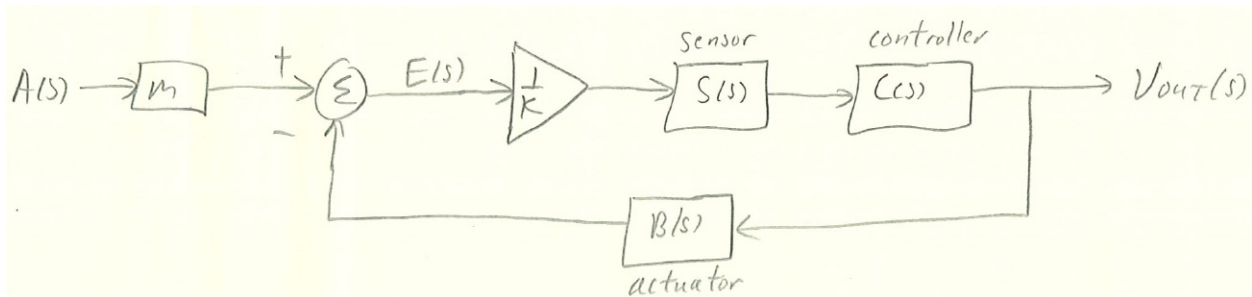
$V_{OUT}(t)$ is the drive signal for the actuator. It also contains all the information about $a(t)$ and is therefore the output signal of the closed loop accelerometer.

Note: there might be an amplifier between V_{OUT} and the actuator. Since this can often be modelled as a simple gain, it could be included in the actuator block.

It is useful to find a transfer function relating $V_{OUT}(t)$ to $a(t)$:

$$\frac{V_{OUT}}{A}(s) = G(s)$$

To do this, we will assume each block has a sufficiently accurate linear model so that we can take its Laplace Transform:



$$E(s) = A(s)m - V_{OUT}(s)B(s) \quad (1)$$

$$V_{OUT}(s) = E(s) \left(\frac{1}{k} \right) S(s)C(s) \quad (2)$$

$$\text{Rewrite (2): } E(s) = \frac{V_{OUT}(s)k}{S(s)C(s)} \quad (3)$$

$$\text{Then (1) } \rightarrow \text{(3): } \frac{V_{OUT}(s)k}{S(s)C(s)} = A(s)m - V_{OUT}(s)B(s)$$

$$\text{Or: } V_{OUT}(s) \left(\frac{k}{S(s)C(s)} + B(s) \right) = A(s)m$$

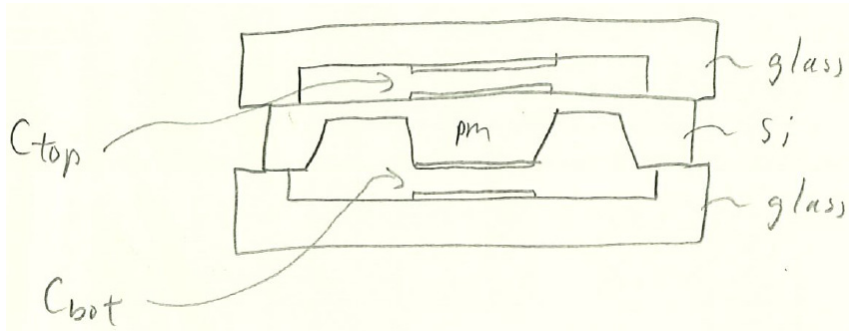
$$\text{Then: } G(s) = \frac{V_{OUT}}{A}(s) = \frac{m}{\frac{k}{S(s)C(s)} + B(s)}$$

$$\text{Now: } V_{OUT}(s) = A(s)G(s)$$

$$\text{And } V_{OUT}(t) = L^{-1}[A(s)G(s)]$$

a. Sensors and actuators

For a vertical motion proof mass architecture, a differential capacitor structure can be used for both sensing *and* actuation:



Let \bar{V}_1 be a high voltage, low frequency signal: for PPA actuation.

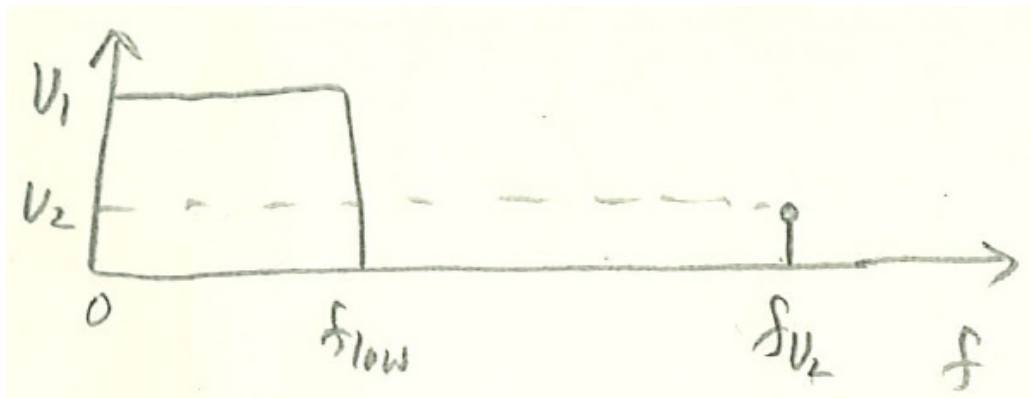
Note: “high voltage” here could mean 100 V, and low frequency might be 1 kHz.

Let \bar{V}_2 be a low voltage, high frequency signal: for $d(t)$ sensing.

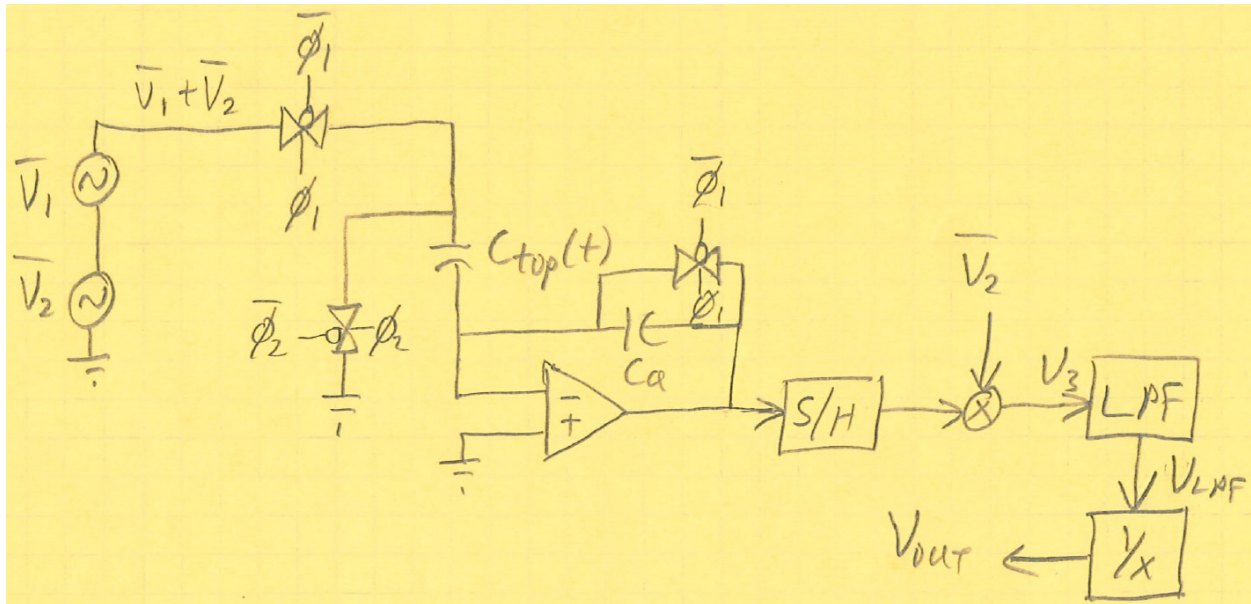
Note: “low voltage” here could be 1 V, and high frequency might be 50 kHz.

\bar{V}_1 is typically over a small bandwidth, while \bar{V}_2 is a sinusoid.

\bar{V}_1 and \bar{V}_2 are added together to realize the following spectral content:



Consider this circuit:



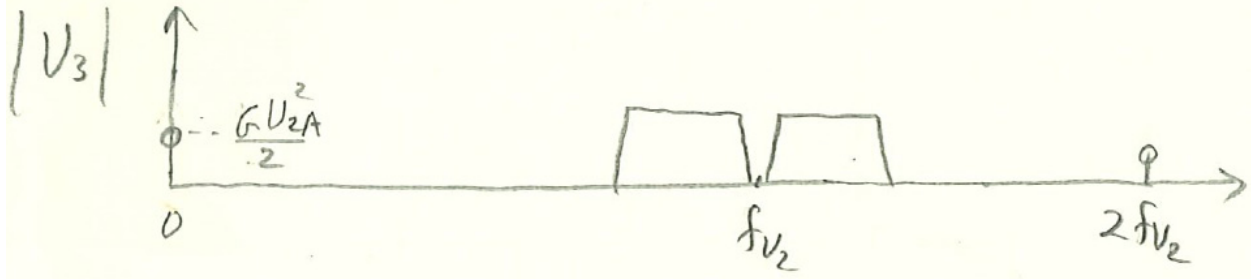
This interface / PPA drive circuit is for one side only. The other side (other PPA) would have a similar circuit. $C_{top}(t)$ and C_a , along with the AC analog switches (little triangles with the dot and the ϕ and $\bar{\phi}$ drive signals) form a charge amplifier with the input signals being \sim AC. Actually, \bar{V}_1 is really time varying DC, while \bar{V}_2 is single frequency AC.

S/H is a sample and hold circuit so that the signal into the mixer is continuous.

The fundamental frequency of ϕ and $\bar{\phi}$ is much higher than the \bar{V}_2 frequency, maybe 200 kHz.

So, the input voltage to the mixer is approximately: $\frac{C_{top}(t)(\bar{V}_1 + \bar{V}_2)}{C_a}$, with high frequency switching noise from ϕ and $\bar{\phi}$. This voltage is mixed with \bar{V}_2 to produce V_3 , which is low pass filtered to produce V_{LPF} .

The spectral content of V_3 is approximately (ignoring ϕ and $\bar{\phi}$ components):



The DC term is recovered by the LPF, yielding:

$$V_{LPF}(t) \approx \frac{GV_{2A}^2}{2} = \frac{V_{2A}^2}{2} \frac{C_{top}(t)}{C_a} = \frac{V_{2A}^2}{2} \frac{\epsilon_0 \epsilon_r A}{C_a d(t)},$$

where $\bar{V}_2 = V_{2A} \cos(\omega t)$.

Notice that $V_{LPF}(t) \propto \frac{1}{d(t)}$, which is not a linear function.

Therefore a $1/x$ analog circuit is used to produce V_{OUT} , so that:

$$V_{OUT}(t) = \frac{2C_a}{V_{2A}^2 \epsilon_0 \epsilon_r A} d(t) = k_1 d(t)$$

This $d(t)$ sensor and interface circuit is compatible with Laplace transforms.

Since the PPA can only pull, not push, only the PPA needed to pull the proof mass would be actuated at any given time. Either or both PPA capacitors could be used to measure $d(t)$ though.

Since there are a lot of different frequency components being input to the mixer, it should be a high-quality mixer with minimal intermodulation products (spurious frequency components generated when two or more signals pass through a non-linear device) so that these unwanted signals do not become part of the $V_{out}(t)$ signal.

The PPA is clearly not a linear device. In order to use Laplace Transforms, a linear model would be needed for it. This could be obtained with a Taylor series approximation for it. However, keep in mind that our linear control system model only approximates the actual nonlinear system...

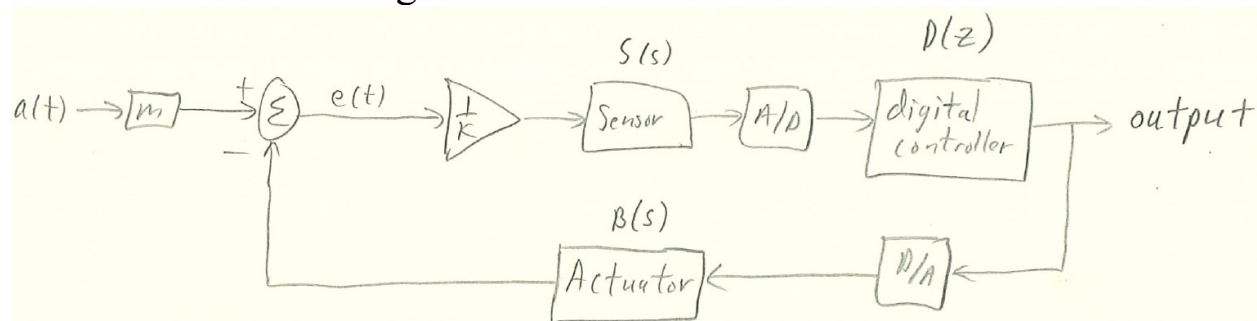
A similar approach would be taken with a lateral closed-loop accelerometer architecture.

2) Digital closed loop accelerometers

Portions of the analog feedback controller can be replaced with a digital controller, enabling some additional features.

a. Traditional digital implementation

Consider the block diagram of the controller shown below:



The digital controller can be implemented on a microcontroller in software or in programmable logic circuitry (FPGA, PLA, etc.). An advantage of this implementation is that the digital controller can easily be modified by changing the programming.

A/D and D/A converters are used to connect the digital controller to the rest of the analog system.

Also, instead of just Laplace transforms being used, z transforms are used in modeling the system.

b. Binary digital controller

This implementation uses a sigma-delta ($\Sigma\Delta$) controller:

Both PPA's are driven with high frequency voltage pulses, where $\omega_p \gg \omega_n$. The SMD responds to the DC average of the force produced by the PPAs.

At zero applied acceleration, both opposing PPA's receive the same number of voltage pulses per second. So, both PPA's produce the same force and the proof mass remains in its rest location.

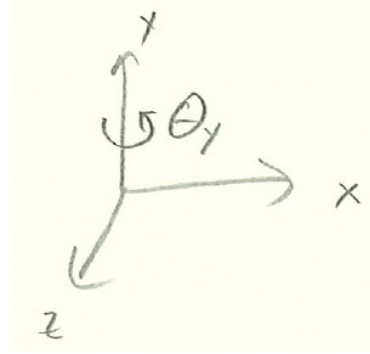
When an acceleration is applied, the proof mass displaces and the displacement is sensed. In response, the PPA whose electrodes are now closer together begins to receive less voltage pulses per second than the other PPA. At this point, the opposing PPA applies a net force on the proof mass to move it back to its rest location.

This controller uses "pulse density modulation," which also contains the information about the acceleration. However, an internal signal that controls the generation of the pulses, rather than the pulses themselves, would be used for the output signal from the accelerometer.

Inertial Sensors (MEMS Gyroscopes)

1) Introduction

Gyroscopes measure angular motion, but not translational motion:



Newton's first law of motion:

An object in translational motion continues in that motion unless it is altered by an external force.

An object in rotational motion continues in that motion unless it is altered by an external torque.

∴ Conservation of momentum: both translational (linear) and rotational (angular).

a. Macroscale gyroscopes

These gyroscopes use a large spinning mass and conservation of angular momentum to measure the angular rate of precession (off axis rotation rate of the spinning object due to an applied torque).

b. Microscale gyroscopes

The most common approach for these gyroscopes is to use a small mass and vibrate it in one direction and then detect orthogonal in-plane motion due to angular rotation about the 3rd axis → due to the Coriolis acceleration, a_c .